# UCLA STAT 110A Applied Statistics - Midterm Review Solutions Observational Studies, Designed Experiments & Surveys

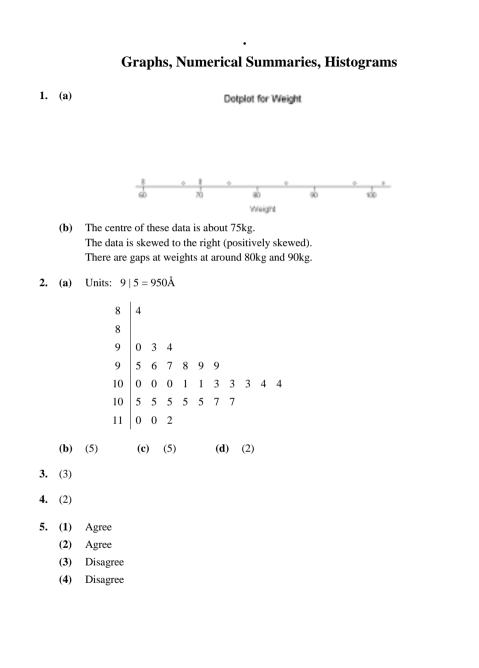
- (i) The treatment being compared is: Study 1: the number of storeys from which the cat fell. Study 2: the gender of the student. Study 3: the style of the commercial.
   (ii) Study 1 at the provide the true of the student.
  - (ii) Study 1: An observational study. There is no allocation (by the researcher) of cats to the number of storeys of the fall. Results are simply observed for cases that happen.
    Study 2: An observational study. There is no allocation (by the researcher) of subjects (the students) to the groups (male or female).
    Study 3: An experiment. The researcher allocates which commercial is to be watched by each subject (shopper).
  - (iii) It is not possible to do an experiment for study 1 due to ethical and moral considerations. To do an experiment a sample of cats would have to be allocated a height and then thrown out of a window at that height.

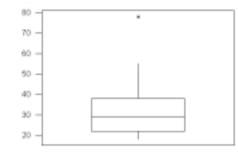
It is not possible to do an experiment for study 2 as the researcher cannot allocate a gender to a student.

- **2.** (5)
- **3.** (3)

**4.** (4)

- 5. Self-selection, selection bias.
- 6. (i) False. A sample of 500 is large enough to give a useful indicative result.
  - (ii) True. Homeless people cannot be contacted by telephone.
  - (iii) True. Telephone polls will usually have some non-response bias. There is no indication of how vigorously non-respondents were followed up.
  - (iv) False. Control groups are not necessary in polls or surveys. Control groups are often used when comparisons want to be made (ie, in observational studies and experiments).
- **7.** (2)





- 7. (1) Disagree, the skew is only moderate.
  - (2) Disagree, the interquartile range is 16.
  - (3) Agree.
  - (4) Agree.
  - (5) Disagree.
- **8.** (1)

6.

- **9.** (2)
- **10.** (3)
- **11.** (3)

## **Exploratory Tools for Relationships**

Section A: Types of Variables

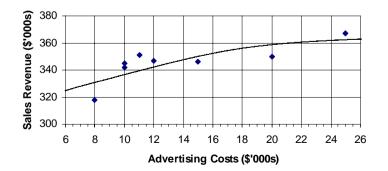
- 1. (a) Quantitative variables are <u>measurements</u> and counts.
  - (b) Qualitative variables describe group membership.
- 2. (a) Variables with few repeated values are treated as continuous.
  - (b) Variables with many *repeated values* are treated as <u>discrete</u>.
- 3. (a) Variables with order are called <u>ordinal</u>.
  - (b) Variables without order are called <u>categorical</u>.
- 4. (a) To explore the relationship between two quantitative variables we use a <u>scatter plot</u>.
  - (b) To explore relationships between a qualitative variable and a quantitative variable we use <u>dot</u> plots, <u>stem-and-leaf</u> plots and <u>box</u> plots.
  - (c) To explore the relationship between two qualitative variables we use a <u>two-way table</u> of <u>counts</u>.

#### Section B: Two Variables



- **2.** (3)
- **3.** (5)
- 4.

### Sales Revenue versus Advertising Costs



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#### Interpretation:

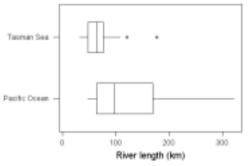
As advertising costs increase, sales revenue also increases. The relationship is not linear – the increase in sales revenue decreases as advertising costs increase. There are no outliers in this data. The amount of scatter about the trend curve is small.

#### 5. (a) Pacific Ocean rivers:

Med = 97 $Q_1 = 64$  $Q_3 = 169$ **Tasman Sea rivers:**Med = 64 $Q_1 = 48$  $Q_3 = 76$ 

(b)

Lengths of Major Rivers in the South Island



Note: For the rivers flowing into the Pacific Ocean:

 $IQR = 105, 1.5 \times IQR = 157.5, Q_3 + 1.5 \times IQR = 326.5, Q_1 - 1.5 \times IQR = -93.5$ 

There are no outside values, the whiskers end at 48 (lower) and 322 (upper).

For the rivers flowing into the Tasman Sea:

 $IQR = 28, 1.5 \times IQR = 42, Q_3 + 1.5 \times IQR = 118, Q_1 - 1.5 \times IQR = 6$ 

177 and 121 are outside values, the whiskers end at 32 (lower) and 108 (upper).

(c) On average, the rivers flowing into the Pacific Ocean are longer.

The lengths of the rivers flowing into the Pacific Ocean have a larger spread than the lengths of the rivers flowing into the Tasman Sea.

The lengths of the rivers flowing into the Pacific Ocean are skewed to the right (positively skewed).

The Grey River and Buller River are outliers amongst the rivers flowing into the Tasman Sea.

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### **Continuous Random Variables**

#### Section A: Probability Density Function Quiz

- 1. Areas under the density curve represent probabilities. The probability that a random observation falls between *a* and *b* is equal to the area between the density curve and the *x*-axis from x = a and x = b.
- 2. The total area under the curve equals 1.
- 3. The population mean  $\mu$  is the point where the density curve balances.
- 4. No, because for a continuous random variable:
- $pr(a \le X \le b) = pr(a < X \le b) = pr(a \le X < b) = pr(a < X < b) = area under the curve between a and b.$
- 5. The curve is bell-shaped, symmetrical and centred at  $\mu$ . The standard deviation  $\sigma$  governs the spread.
- 6. The parameters are  $\mu$  and  $\sigma$ .

### Section B: Normal Distribution

- **1.** (a) pr(X < 245) = 0.0947
  - (b) pr(255 < X < 280) = pr(X < 280) pr(X < 255) = 0.8092 0.2459 = 0.5633
  - (c) pr(X > 287) = 1 pr(X < 287) = 1 0.9053 = 0.0947
- 2. Let *X* be the survival time in months of a cancer patient on this drug.
  - (a) (i)  $pr(X \le 12) = 0.1163$ 
    - (ii) pr(12 < X < 24) = pr(X < 24) pr(X < 12) = 0.3286 0.1163 = 0.2123
    - (iii) pr(X > x) = 0.8 therefore pr(X < x) = 0.2 and so x = 17.6341. 80% of the patients live beyond 17.6 months.
    - (iv) pr(a < X < b) = 0.8
      - pr(X < a) = 0.1 and so a = 10.5932
      - pr(X < b) = 0.9 and so b = 51.6048

The range of the central 80% of survival times is from 10.6 to 51.6 months.

- (b) There are some doubts about the validity of the assumption that survival times are Normally distributed. Although the data is roughly symmetrical, there is a gap in the centre which could indicate bimodality of survival times. The tails seem too short for the underlying distribution to have a Normal distribution.
- 3. Let *X* be the maximum distance reached by a pilot without moving the seat.
  - (a)  $\operatorname{pr}(X \ge 120) = 1 \operatorname{pr}(X \le 120) = 1 0.3085 = 0.6915$
  - (b)  $pr(X \ge x) = 0.95$  therefore pr(X < x) = 0.05 and so x = 108.5515.

The maximum distance at which the switch should be placed is 109cm.

- (c) (i) That this pilot's maximum reach is 1.5 standard deviations above the mean.
  - (ii)  $x = 125 + 1.5 \times 10 = 140$ cm. A z-score of 1.5 corresponds to a maximum reach of 140cm.

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#### Section C: Combining Random Variables

- W 3 X 2 Y 1. (a) х х = Т 3 Χ -2 **(b)** \_ х х VY (c) 1 х = 2. (4) **3.** (1) 4. (5) 5. (1) 6. (a) Let G be the charge for a randomly chosen gardening job.  $G_i \sim \text{Normal} (\mu = 25, \sigma = 3)$  $X = G_1 + G_2 + G_3 + G_4 + G_5 + G_6$  $E(X) = E(G_1 + G_2 + G_3 + G_4 + G_5 + G_6) = 6 \times E(G_i) = 6 \times 25 = 150$  $sd(X) = sd(G_1 + G_2 + G_2 + G_4 + G_5 + G_6) = \sqrt{6} \times sd(G_2) = \sqrt{6} \times 3 = 7.35$ (b) (i) Let  $M_i$  be the charge for a randomly chosen moving job.  $M_i \sim \text{Normal} (\mu = 15, \sigma = 2)$  $Y = M_1 + M_2 + \ldots + M_{11}$  $E(Y) = E(M_1 + M_2 + ... + M_{11}) = 11 \times E(M_i) = 11 \times 15 = 165$  $sd(Y) = sd(M_1 + M_2 + ... + M_{11}) = \sqrt{11} \times sd(M_i) = \sqrt{11} \times 2 = 6.63$ (ii) T = X + Y(iii) T has a Normal distribution because it is a combination of Normally distributed random variables. (iv) E(T) = E(X + Y) = E(X) + E(Y) = 150 + 165 = 315 $sd(T) = sd(X + Y) = \sqrt{sd(X)^2 + sd(Y)^2} = \sqrt{7.35^2 + 6.63^2} = 9.90$ In order to calculate the standard deviation of T we had to assume that X and Y are independent random variables. (c) Let M be the charge for a randomly chosen moving job.  $M \sim Normal (\mu = 15, \sigma = 2)$ 
  - (c) Let *M* be the charge for a randomly chosen mowing job.  $M \sim \text{Normal} (\mu = 15, \sigma = W = 52M)$

 $E(W) = 52E(M) = 52 \times 15 = 780$ sd(W) = |52|sd(M) = 52 × 2 = 104 W ~ Normal( $\mu$  = \$780,  $\sigma$  = \$104)

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7. Let *M* be the morning travel time and *N* be the evening travel time.

assuming independence of ten travel times in the week.