UCLA STAT 110 A
Applied Statistics

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UCLA STAT 110A
Applied Statistics

Course Description,
Class homepage,
online supplements, VOH's etc.

http://www.stat.ucla.edu/~dinov/

What is Statistics? A practical example

●*Demography: Uncertain population forecasts*
by Nico Keilman, Wolfgang Lutz, *et al.,* Nature 412, 490 - 491 (2001)

●Traditional population forecasts made by statistical agencies **do not quantify uncertainty**. But demographers and statisticians have developed methods to calculate probabilistic forecasts.
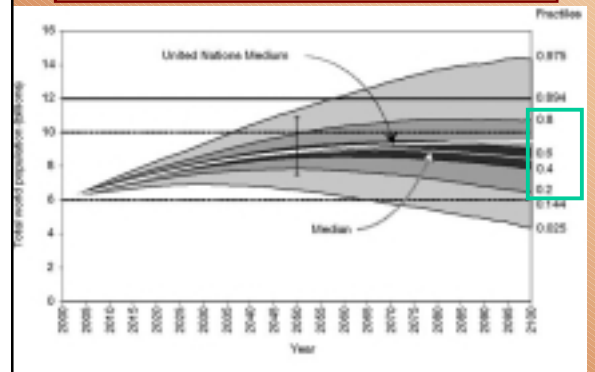
●The demographic future of any human population is uncertain, but some of the many possible trajectories are more probable than others. So, forecast demographics of a population, e.g., size by 2100, should include two elements: a range of possible outcomes, and a probability attached to that range.

What is Statistics?

●Together, ranges/probabilities constitute a *prediction interval* for the population. There are trade-offs between greater certainty (higher odds) and better precision (narrower intervals). Why?

●For instance, the next table shows an estimate that the odds are 4 to 1 (an 80% chance) that the world's population, now at 6.1 billion, will be in the range [5.6 : 12.1] billion in the year 2100. Odds of 19 to 1 (a 95% chance) result in a **wider** interval: [4.3 : 14.4] billion.

Table 1 Forecasted population sizes and proportions over age 60

Year	Median world and regional population sizes (millions)				
	2000	2025	2050	2075	2100
World total	6,055	7,827 (7,219–8,459)	8,797 (7,347–10,443)	8,951 (6,636–11,652)	8,414 (5,577–12,123)
North Africa	173	257 (228–285)	311 (249–378)	336 (238–443)	333 (215–484)
Sub-Saharan Africa	611	976 (856–1,100)	1,319 (1,010–1,701)	1,522 (1,021–2,194)	1,500 (878–2,450)
North America	314	379 (351–410)	422 (358–498)	441 (343–565)	454 (313–631)
Latin America	515	709 (643–775)	840 (679–1,005)	904 (647–1,202)	934 (585–1,383)
Central Asia	56	81 (73–90)	100 (80–121)	107 (76–145)	106 (66–159)
Middle East	172	285 (252–318)	368 (301–445)	413 (296–544)	413 (259–597)
South Asia	1,367	1,940 (1,735–2,154)	2,249 (1,795–2,776)	2,242 (1,528–3,085)	1,958 (1,186–3,035)
China region	1,408	1,608 (1,494–1,714)	1,580 (1,305–1,849)	1,422 (1,003–1,884)	1,250 (765–1,870)
Pacific Asia	476	625 (569–682)	702 (575–842)	702 (509–937)	654 (410–949)
Pacific OECD	150	155 (144–165)	148 (125–174)	135 (100–175)	123 (79–173)
Western Europe	456	478 (445–508)	470 (399–549)	433 (321–562)	392 (257–568)
Eastern Europe	121	117 (109–125)	104 (86–124)	87 (61–118)	74 (44–115)
European part of the former USSR	236	218 (203–234)	187 (154–225)	159 (110–216)	141 (85–218)

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Large view

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What is Statistics?

Proportion of population over age 60		
2000	2050	2100
0.10	0.22	0.34
	(0.18–0.27)	(0.25–0.44)
0.06	0.19	0.32
	(0.15–0.25)	(0.23–0.44)
0.05	0.07	0.20
	(0.05–0.09)	(0.14–0.27)
0.16	0.30	0.40
	(0.23–0.37)	(0.28–0.52)
0.08	0.22	0.33
	(0.17–0.28)	(0.23–0.45)
0.08	0.20	0.34
	(0.15–0.25)	(0.24–0.46)
0.06	0.18	0.35
	(0.14–0.23)	(0.24–0.47)
0.07	0.18	0.35
	(0.14–0.24)	(0.25–0.48)
0.10	0.30	0.39
	(0.24–0.37)	(0.27–0.53)
0.08	0.23	0.36
	(0.18–0.29)	(0.26–0.49)
0.22	0.39	0.49
	(0.32–0.47)	(0.35–0.61)
0.20	0.35	0.45
	(0.29–0.43)	(0.32–0.58)
0.18	0.38	0.42
	(0.30–0.46)	(0.28–0.57)
0.19	0.35	0.36
	(0.27–0.44)	(0.23–0.50)

● *Demography: Uncertain population forecasts*

by Nico Keilman, Nature 412, ,2001

● Traditional population forecasts made by statistical agencies **do not quantify uncertainty**. But lately demographers and statisticians have developed methods to calculate probabilistic forecasts.

● Proportion of population over 60yrs.

What is Statistics?

What is Statistics?

● There is concern about the accuracy of population forecasts, in part because the rapid fall in fertility in Western countries in the 1970s came as a surprise. Forecasts made in those years predicted birth rates that were up to 80% too high.

● The rapid reduction in mortality after the Second World War was also not foreseen; life-expectancy forecasts were too low by 1–2 years; and the predicted number of elderly, particularly the oldest people, was far too low.

What is Statistics?

● So, during the 1990s, researchers developed methods for making probabilistic population forecasts, the **aim** of which is to calculate prediction intervals for every variable of interest. Examples include population forecasts for the USA, AU, DE, FIN and the Netherlands; these forecasts comprised prediction intervals for variables such as age structure, average number of children per woman, immigration flow, disease epidemics.

● We need accurate probabilistic population forecasts for the whole world, and its 13 large division regions (see Table). The conclusion is that there is an estimated 85% chance that the world's population will stop growing before 2100. Accurate?

What is Statistics?

● There are three main methods of probabilistic forecasting:
time-series extrapolation;
expert judgement; and
extrapolation of historical forecast errors.

● Time-series methods rely on statistical models that are fitted to historical data. These methods, however, seldom give an accurate description of the past. If many of the historical facts remain unexplained, time-series methods result in excessively wide prediction intervals when used for long-term forecasting.

● Expert judgement is subjective, and historic-extrapolation alone may be near-sighted.

Chapter 1: Intro to Data Analysis

● Variation in data
● Data Distributions
● Stationary and (dynamic) non-stationary processes
● Causes of Variation

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Newtonial science vs. chaotic science

- Article by Robert May, Nature, vol. 411, June 21, 2001
  - Science we encounter at schools deals with crisp certainties (e.g., prediction of planetary orbits, the periodic table as a descriptor of all elements, equations describing area, volume, velocity, position, etc.)
  - As soon as uncertainty comes in the picture it shakes the foundation of the deterministic science, because only probabilistic statements can be made in describing a phenomenon (e.g., roulette wheels, chaotic dynamic weather predictions, Geiger counter, earthquakes, etc.)
  - What is then science all about – describing absolutely certain events and laws alone, or describing more general phenomena in terms of their behavior and chance of occurring? Or may be both!

Variation in sample percentages

Poll: Do you consider yourself overweight?

Target: True population percentage = 69%

10 Samples of **20** people

10 Samples of **500** people

We are getting closer to The population mean, as $n \rightarrow \infty$ is this a coincidence?

50   60   70   80   90

Sample percentage

Comparing percentages from 10 different surveys each of 20 people with those from 10 surveys each of 500 people (all surveys from same population).

Experiments vs. observational studies
for comparing the effects of treatments

- In an Experiment
  - experimenter determines which units receive which treatments. (ideally using some form of random allocation)
- Observational study – useful when can't design a controlled randomized study
  - compare units that happen to have received each of the treatments
  - Ideal for describing relationships between different characteristics in a population.
  - often useful for identifying possible causes of effects, but cannot reliably establish causation.
- Only properly designed and executed experiments can reliably demonstrate causation.

The Subject of Statistics

- Statistics is concerned with the process of finding out about the world and how it operates - in the face of variation and uncertainty
- by collecting and analyzing, making sense (interpreting) of data.
- Data are measurements, facts and information about an object or a process that allows is to make inference about the object being observed.

The investigative process

(a)	(b)	(c)	(d)	(e)	(f)
Real problems, curiosity	Questions about world	Design method of data collection	Collect data	Summary and analysis of data	Answers to original questions

The investigative process.

Sources of non-sampling errors

- *Selection bias*:
  Arises when the population sampled is not exactly the population of interest.
- *Self-selection*:
  People themselves decide whether or not to be surveyed. Results akin to severe non-response.
- *Non-response bias*:
  Non-respondents often behave or think differently from respondents
  - low response rates can lead to huge biases.

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Immigration Example

● Suppose that you want to set up a nationwide survey about immigration issues. Think as precisely as you can about the target population that you would be interested in.

-Who would you want included?

-Who would you want excluded?

-Can you define some rules to characterize your target population?

Immigration Example

● We could take all members of the population in the US at the time, who were entitled to vote in national elections. This may exclude the young, the illegal immigrants, those people in prisons and people legally committed to mental institutions. It would include any other permanent residents of the US, whether or not they were citizens, and citizens living overseas.

● You might want to be more, or less, restrictive. In practice, one would probably sample from something like the electoral

● districts [that subset of people who fit the eligibility criteria for voting and who have registered to do so].

● Should the goals of the study influence your survey design (in particular how conservative your selection is)?

Poll Example

● A survey of High School principals taken after a widespread change in the public school system revealed that 20% of them were under stress-reliefe medication, and almost 50% had seen a doctor in the past 6 mo.s with stress complains. The survey was compiled from 250 questionnaires returned out of 2500 sent out. How reliable the results of this experiment are and why?

Poll Example

● This is only a 10% response rate - the people who responded could be very unrepresentative. It could well be that the survey struck a responsive chord with stressed-out principals.

Experimental vs. Observation study

● A researcher wants to evaluate IQ levels are related to person's height. 100 people are are randomly selected and grouped into 5 bins: [0:50], [50;100), [100:150], [150:200), [200:250] *cm* in height. The subjects undertook a IQ exam and the results are analyzed.

● Another researcher wants to assess the bleaching effects of 10 laundry detergents on 3 different colors (R,G,B). The laundry detergents are randomly selected and applied to 10 pieces of cloth. The discoloration is finally evaluated.

Experimental vs. Observation study

● For each study, describe what *treatment* is being compared and what *response* is being measured to compare the treatments.

● Which of the studies would be described as *experiments* and which would be described as *observational* studies?

● For the studies that are observational, could an experiment have been carried out instead? If not, briefly explain why not.

● For the studies that are experiments, briefly discuss what *forms of blinding* would be possible to be used.

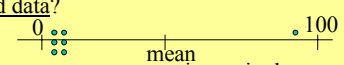● In which of the studies has *blocking* been used? Briefly describe *what* was blocked and why it was blocked.

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Experimental vs. Observation study

- What is the *treatment* and what is the *response?*
  1. Treatment is height (as a bin). Response is IQ score.
  2. Treatment is laundry detergent. Response is discoloration.
- *Experiment* or *observational* study?
  1. Observational – compare obs's (IQ) which happen to have the treatment (height).
  2. Experimental – experimenter controls which treatment is applied to which unit.
- For the observational studies, can we conduct an experiment?
  1. This could not be done as an experiment - it would require the experimenter to decide the (natural) height (treatment) of the subjects (units).
- For the experiments, is there *blinding?*
  2. The only form of blinding possible would be for the technicians measuring the cloth discoloration not to know which detergent was applied.
- Is there *blocking*?
  1. & 2. No blocking. Say, if there are two laundry machines with different cycles of operation and if we want to block we'll need to randomize which laundry does which cloth/detergent combinations, because differences in laundry cycles are a known source of variation.

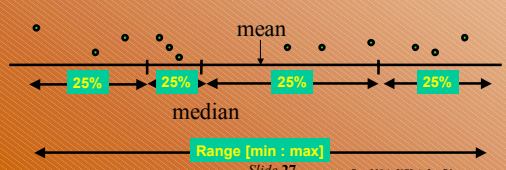## Mean, Median, Mode, Quartiles, 5# summary

- The sample mean is the average of all numeric obs's.
- The sample median is the obs. at the index $(n+1)/2$ (note take avg of the 2 obs's in the middle for fractions like 23.5), of the observations ordered by size (small-to-large)?
- The sample median usually preferred to the sample mean for skewed data?

  0 ⠒⠒ _____ $_\bullet$ 100
  mean

- Under what circumstances may quoting a single center (be it mean or median) not make sense?(multi-modal)
- What can we say about the sample mean of a qualitative variable? (meaningless)

Quartiles

The first quartile (Q_1) is the median of all the observations whose *position* is strictly below the *position* of the median, and the third quartile (Q_3) is the median of those above.

Five number summary

The five-number summery = (Min, Q_1, Med, Q_3, Max)

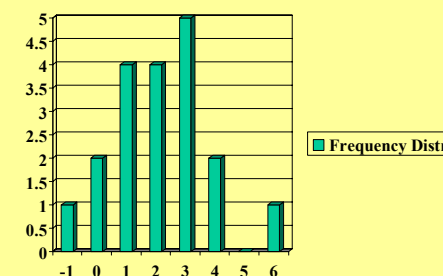## Data Distribution

- A data distribution is a summary of the variation in a dataset. Data distribution is a list of all possible values (of the process/object) and their respective frequencies (e.g., how often is each possible value encountered, when we observe the object/process).
- E.g., {1, 2, 2, 3, -1, 0, 0, 1, 2, 3, 4, 3, 3, 1, 2, 1, 4, 6, 3}

Data Distribution

- E.g., {1, 2, 2, 3, -1, 0, 0, 1, 2, 3, 4, 3, 3, 1, 2, 1, 4, 6, 3}

Stationarity of Processes

- Does the variability of the data change significantly as more data is collected (say between different time points, different physical locations, etc.)?
- **Stationary process** is a data-generating mechanism for which the distribution of the resulting data does NOT change appreciably as more data is being observed.
- **Non-Stationary process** is a data-generating mechanism for which the distribution of the resulting data DOES change as more data is being observed.
- E.g., Grades (over time), Air quality (in different regions in the US), Geiger counter (time), Species Extinction (long-times). Other examples?

Stationary or Non-Stationary Process?

- **Histograms?** Do not work too well. Why?

Data: elece1.xls

Stationary or Non-Stationary Process?

- **Histograms?** Do not work too well. Why?

Stationary or Non-Stationary Process?

- **Histograms?** Do not work too well. Why? (Cumulative counts!)
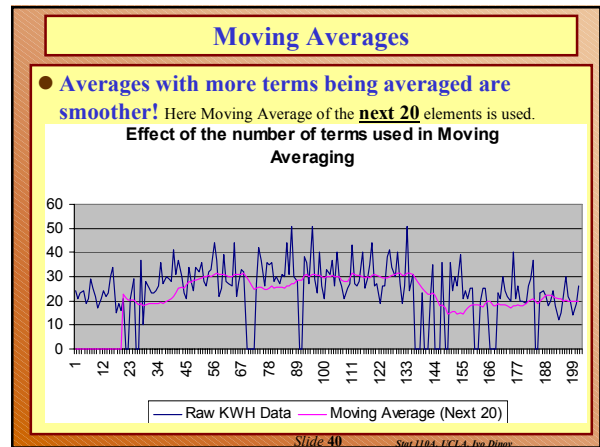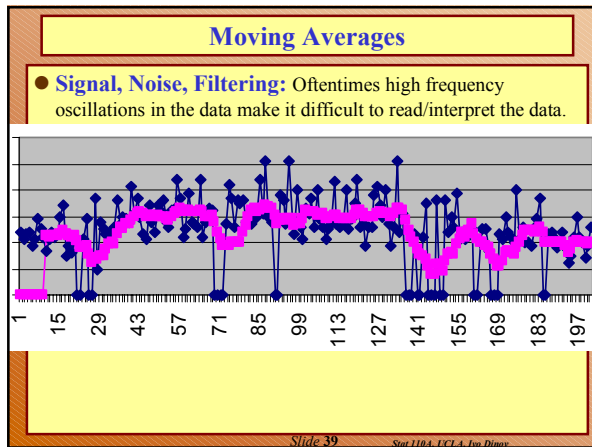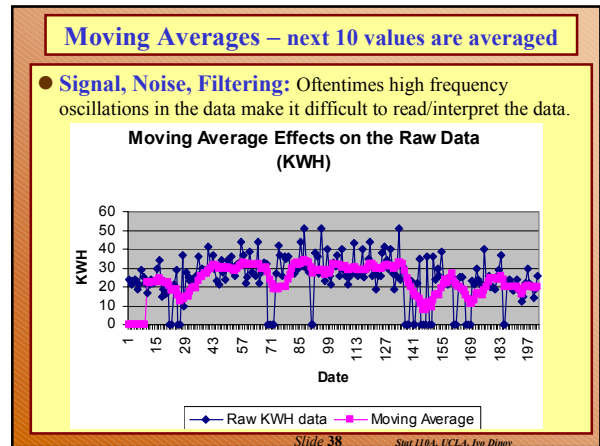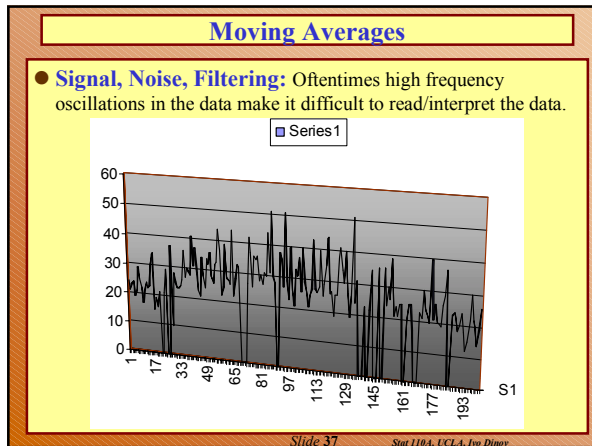
Stationary or Non-Stationary Process?

- **To assess stationarity:**
- **Rigorous assessment:** A stationary process has a constant mean, variance, and autocorrelation through time/place.
- **Visual assessment:** (Plot the data – observed vs. time/place, etc., – parameter we argue stationarity with respect to).

Stationary or Non-Stationary Process?

- **Visual assessment:** (Plot the data – observed vs. time/place, etc., – parameter we argue stationarity with respect to).

6

Moving Averages

- **Signal, Noise, Filtering:** Oftentimes high frequency oscillations in the data make it difficult to read/interpret the data.

Moving Averages – next 10 values are averaged

- **Signal, Noise, Filtering:** Oftentimes high frequency oscillations in the data make it difficult to read/interpret the data.

Moving Average Effects on the Raw Data (KWH)

Moving Averages

- **Signal, Noise, Filtering:** Oftentimes high frequency oscillations in the data make it difficult to read/interpret the data.

Moving Averages

- **Averages with more terms being averaged are smoother!** Here Moving Average of the **next 20** elements is used.

**Effect of the number of terms used in Moving Averaging**

Causes of Variation in Data

- Cause of variation is the reason/mechanism that introduces some of the observed variation in the data.
- Kinds of causes of variation:
  - Common cause – the inherented fluctuations in a process, e.g., Geiger counter variances, random arrival time variances
  - Special causes – periodically/cyclically arising variances, e.g., temp measures vary with season, wake-up times vary specially with day-of-week (weekends most people sleep longer), different machine settings/protocols (MRI imaging).

Causes of Variation in Data

- E.g., Washer Thickness: Data: washer5.dat (SYSTAT)

Washer Thickness 3 Machines
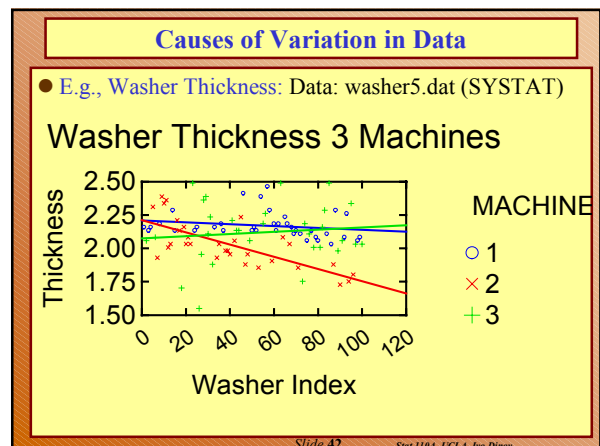
Causes of Variation in Data –
Stratified Plots for identifying causes of variation

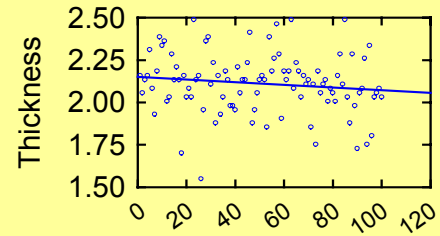● E.g., Washer Thickness: Data: washer5.dat (SYSTAT)
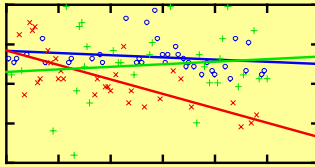
MACHINE

○ 1
× 2
+ 3

● Machine 1 exhibits normal operating conditions (variation purely due to common causes). Machine 3 shows abnormal cyclic variation. Machine 2 shows a consistent robust thickness decline – special causes variability.

Causes of Variation in Data

● E.g., Washer Thickness: Data: washer5.dat (SYSTAT)

● If you plot all washer thicknesses all together you may miss the facts that there are special cause effects on the variances.