

UCLA STAT XL 10 Introduction to Statistical Reasoning

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Chapter 6 – Measurement Error, Chance and Uncertainty

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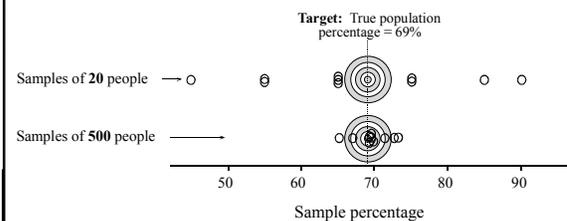
Newtonial science vs. chaotic science

- Article by Robert May, Nature, vol. 411, June 21, 2001
 - Science we encounter at schools deals with **crisp certainties** (e.g., prediction of planetary orbits, the periodic table as a descriptor of all elements, equations describing area, volume, velocity, position, etc.)
 - As soon as **uncertainty** comes in the picture it **shakes the foundation of the deterministic science**, because only **probabilistic statements** can be made in describing a phenomenon (e.g., roulette wheels, chaotic dynamic weather predictions, Geiger counter, earthquakes, Others?)
 - **What is then science all about** – describing absolutely certain events and laws alone, or describing more general phenomena in terms of their behavior and chance of occurring? Or may be both!

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Variation in sample percentages



Comparing percentages from 10 different surveys each of 20 people with those from 10 surveys each of 500 people (all surveys from same population).

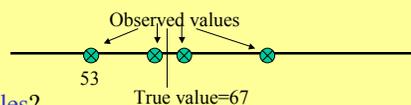
From Chance Encounters by C.J. Wild and G.A.F. Seber, © John Wiley & Sons, 2000.

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Measurement Error

- No matter how carefully a measurement of a single unit is made it often comes out a bit different. Do repeated measurements to find out by how much different each observation is!
- The SD of a series of repeated measurements estimates the **likely size of the chance error** in a single measurement of the process being observed.



● **Examples?**

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Random or chance error ...

- **Random or chance error** is the difference between the **sample-value** and the **true population-value** (e.g., 53 vs. 67, in the above example).

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The Subject of **Statistics**

Statistics is concerned with the process of finding out about the world and how it operates -

- in the face of **variation** and **uncertainty**
- by **collecting** and then **making sense** (interpreting, summarizing) of data.

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The investigative process

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Questions

- What are two ways in which random observations arise and give examples. (random sampling from finite population – randomized scientific experiment; random process producing data, observational data, surveys.)
- What is a **parameter**? Give two examples of parameters. (characteristic of the data – mean, 1st quartile, std.dev.)
- What is an **estimate**? How would you estimate the parameters you described in the previous question?
- What is the distinction between an **estimate** (p^\wedge value calculated from obs'd data to approx. a parameter) and an **estimator** (P^\wedge abstraction the the properties of the ransom process and the sample that produced the estimate) ? Why is this distinction necessary? (effects of sampling variation in P^\wedge)

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Observable data

- **Individual Measurements =**
Exact Value +
Bias +
Chance Error
(an effect that consistently moves all observations up/down)
- **Examples?**

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Review

- Let $\{x_{1,1}, x_{1,2}, x_{1,3}, \dots, x_{1,N}\}$
 $\{x_{2,1}, x_{2,2}, x_{2,3}, \dots, x_{2,N}\}$
 \dots
 $\{x_{K,1}, x_{K,2}, x_{K,3}, \dots, x_{K,N}\}$

K samples of size N. Data comes from a distr'n with μ, σ , but we're interested in mean/std-dev of **sample average**

- As the number of samples and the number of observations within each sample increase we get a better estimate of the true population parameter (say the mean). Scottish soldiers chest measurements example ...

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The sample mean has a **sampling distribution**

Sampling batches of 6 Scottish soldiers and taking chest measurements. Population $\mu = 39.8$ in, and $\sigma = 2.05$ in.

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Standard error of an estimate

The *standard error* of any estimate $\hat{\theta}$ [denoted $se(\hat{\theta})$]

- estimates the variability of $\hat{\theta}$ values in repeated sampling and
- is a measure of the *precision* of $\hat{\theta}$. Example: \bar{X} , as an estimator of the population mean, μ .

$$SE(\bar{X}) = \frac{\sigma}{\sqrt{n}}, \text{ where } \bar{X} = \frac{1}{n} \sum_{k=1}^n X_k, \text{ and}$$

σ is the standard deviation of $\{X_k\}$, $1 \leq k \leq n$.

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Review

- What is meant by the terms **parameter** and **estimate**.
- Is an estimator a RV?
- What is **statistical inference**? (process of making conclusions or making useful statements about unknown distribution parameters based on observed data.)
- What are **bias** and **precision**?
- What is meant when an estimate of an unknown parameter is described as **unbiased**?

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