

Stat13 Homework 3

http://www.stat.ucla.edu/~dinov/courses_students.html

(30 points, student scores will be converted to scores out of 100)

Suggested Solutions

Problem 1 (15 points)

X = number of malfunction disk drives

$X \sim \text{Binomial}(n, p)$

$$P(X=x) = \binom{n}{x} p^x (1-p)^{n-x} \text{ where } \binom{n}{x} = \frac{n!}{x!(n-x)!}$$

A, $n = 10$ (1 pt), $p = 4\% = 0.04$ (1pt)

B, Assumptions:

- each trial has only 2 outcomes: function / malfunction (1 pt)

- constant $p \Rightarrow$ same value for each trial (1 pt)

- independence \Rightarrow results are independent of each other (1 pt)

C, Yes (1 pt)

D,

$$\text{Notation: } nCr = \binom{n}{r}$$

1, $P(X=0) = {}_{10}C_0 * (0.04)^0 * (0.96)^{10} = 0.6648$ (2 pts)

2, $P(X=1) = {}_{10}C_1 * (0.04)^1 * (0.96)^9 = 0.277$ (2 pts)

3, $P(X \geq 2) = 1 - P(X < 2) = 1 - P(X \leq 1) = 1 - [P(X=0) + P(X=1)] = 1 - [0.6648 + 0.277] = 0.0582$ (2 pts)

4, $P(3 \leq X \leq 6)$: (3 pts)

method 1:

$$= P(X=3) + P(X=4) + P(X=5) + P(X=6) = 0.006213$$

method 2:

$$= P(X \leq 6) - P(X < 3)$$

$$= P(X \leq 6) - P(X \leq 2)$$

$$= 0.999999982331 - 0.993786284008$$

$$= 0.006213$$

Problem 2 (10 points)

Notation: Hus B = husband's blood type B

A, Since husband's blood type independent of wife's blood type,

$$P(\text{Hus B}) = 11\% \text{ (1 pt)}$$

B, Due to independence,

$$P(\text{Hus A and Wife A}) = P(\text{Hus A}) * P(\text{Wife A}) = 30\% * 30\% = 9\% \text{ (2 pts)}$$

C, $P(\text{at least 1 AB})$: (3 pts)

Method 1:

$$= P(\text{Hus not AB and Wife AB}) + P(\text{Hus AB and Wife not AB}) + P(\text{Hus AB and Wife AB})$$

$$= (90\%) (10\%) + (10\%) (90\%) + (10\%) (10\%) = 19\%$$

Method 2: (Using complement rule)

$$= 1 - P(\text{Hus not AB and Wife not AB})$$

$$= 1 - (90\%)(90\%) = 19\%$$

D, P(same blood type) = P(Hus O and Wife O) + P(Hus A and Wife A) + P(Hus B and Wife B) + P(Hus AB and Wife AB)

$$= (49\%)(49\%) + (30\%)(30\%) + (11\%)(11\%) + (10\%)(10\%)$$

$$= 35.22\% \text{ (4 pt)}$$

Problem 3 (5 points)

Total number of members = 275

Total number of females = 150

Total number of males = 125

A, P(female) = $150/275 = 0.545$ (1 pt)

B, P(female and 4-5 times) = $37/275 = 0.1345$ (1 pt)

C, P(male or 4-or-more) = $P(\text{male}) + P(4\text{-or-more}) - P(\text{male and } 4\text{-or-more})$

$$= 125/275 + (26+6+37+11)/275 - (26+6)/275$$

$$= 173/275$$

$$= 0.629 \text{ (3 pts)}$$

OR

$$P(\text{male or 4-or-more}) = 1 - P(\text{Complement}) = 1 - P(\text{Female and in group-A-or-B})=$$

$$= 1 - P(\{ \text{Female and in group-A} \} \text{ or } \{ \text{Female and in group-B} \})=$$

$$= 1 - (34/275 + 68/275) = 1 - 0.371$$

$$= 0.629 \text{ (3 pts)}$$