# UCLA STAT 13

Introduction to Statistical Methods for the Life and Health Sciences

> Instructor: IVO Dinov, Asst. Prof. of Statistics and Neurology

# Teaching Assistants:

## Jacquelina Dacosta & Chris Barr

University of California, Los Angeles, Fall 2006 http://www.stat.ucla.edu/~dinov/courses\_students.html Sample Size Calculations & Confidence Intervals for Proportions

# Planning a Study to Estimate $\mu$

• It is important before you begin collecting data to consider whether the estimates will be sufficiently precise.

- Two factors to consider:
  - the population variability of Y
  - sample size

## Planning a Study to Estimate $\mu$

• First: In certain situations the variability of Y should not be controlled for (response in a medical study to treatment). However, in most studies it is important to reduce the variability of Y, by holding extraneous conditions as constant as possible.

For example: study of breast cancer might want to examine only women

# Planning a Study to Estimate $\mu$

• Second: Once the experiment is planned to reduce the variability of Y as much as possible, we consider the sample size.

For example: how many women should we sample to achieve the desired precision for our estimate?

• RECALL:  $SE = \frac{s}{\sqrt{n}}$ 

# Planning a Study to Estimate $\mu$

• To decide on a proper value of n, we must specify what value of SE is desirable and have a guess of s.

For SE we need to ask what value would we tolerate?
 For s we could use information from a pilot study or previous research

Desired SE = 
$$\frac{Guessed \ s}{\sqrt{n}}$$





2SE = 1.2

SE = 0.6





### Conditions of validity of the SE formula

 Definition: A hierarchical structure exists when observations are nested within the sampling units
 this is a common problem in the sciences

Example: Measure the pulse of 10 patients 3 times each.

- We don't have 30 pieces of independent information.
  - One possible naïve solution: we could use each persons average

# Conditions of validity of a CI for $\mu$

 Data must be from a random sample and observations must be independent of each other

If the data is biased, the sampling distribution concepts on which the CI method is based do not hold

knowing the average of a biased sample does not provide information about  $\mu$ 

## Conditions of validity of a CI for $\mu$

- We also need to consider the shape of the data for Student's T distribution:
  - If Y is normally distributed then Student's T is exactly valid
     If Y is approximately normal then Student's T is
  - approximately valid
  - If Y is not normal then Student's T is approximately valid only if n is large (CLT)
  - ☐ How large? Really depends on severity of non-normality, however our rule of thumb is n ≥ 30
  - Page 202 has a nice summary of these conditions
  - **NOTE:** If sampling distribution cannot be considered normal Student's T will not hold.

Slide 15

#### Depossible bias

non-independent observations

Scrutinize study design for:

**Verifications of Conditions** 

In practice these conditions are often

assumptions, but it is important to check to make

Population Normal?

sure they are reasonable

random sampling

- previous experience with other similar data
- histogram/normal probability plot
- □ increase sample size
- try a transformation and analyze on the transformed scale
  Slide 16
  Stat 13 UCLA tra Dirac

# **CI for a Population Proportion**

 So far we have discussed a confidence interval using quantitative data

• There is also a CI for a dichotomous categorical variable when the parameter of interest is a population proportion

 $\hat{p}$  is the sample proportion p is the population proportion

### **CI for a Population Proportion**

- When the sample size is large, the sampling distribution of p̂ is approximately normal
   Related to the CLT
- When the sample size is small, the normal approximation may be inadequate
  - **To accommodate this we will modify**  $\hat{p}$  slightly

## **CI for a Population Proportion**

• The adjustment we are going to make to  $\hat{p}$  is to use  $\tilde{p}$  instead

$$\hat{p} = \frac{y}{n} \longrightarrow \tilde{p} = \frac{y + 0.5 \left( z_{\alpha/2}^2 \right)}{n + \left( z_{\alpha/2}^2 \right)}$$

• Relax and remember that the formula for  $\hat{p}$  was:

$$\hat{p} = \frac{y}{n}$$







## CI for a Population Proportion

Incorporate that logic and we get:

$$\widetilde{p} \pm z_{\alpha/2} \left( SE_{\widetilde{p}} \right)$$

Where  $100(1 - \alpha)$  is the desired confidence This time we will use a z multiplier instead of a t multiplier















