UCLA STAT 13

Introduction to Statistical Methods for the Life and Health Sciences

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Parameters and Statistics

Variables can be summarized using statistics.

- **Definition**: A *statistic* is a numerical measure that describes a characteristic of the sample.
- **Definition**: A *parameter* is a numerical measure that describes a characteristic of the population.
- We use statistics to estimate parameters

Measures of Centrality

- Recall that center is #2 of the BIG three.
- Measures of center include:
 - the mean
 - the median
 - the mode (the value with the highest frequency)

• These measures all describe the center of a distribution in a slightly different way

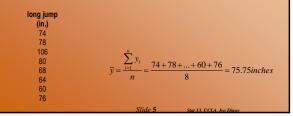
Measures of Center

The Mean
aka the average
can be thought of as the balancing point of a distribution

$$\overline{y} = \frac{\sum_{i=1}^{n} y_i}{n}$$

Measures of Center

Example: In an experiment with some statistics students, 8 male students were randomly selected and asked to perform the standing long jump. In reality every student participated, but for the ease of calculations below we will focus on these eight students. The long jumps were as follows:



Measures of Center

The Median

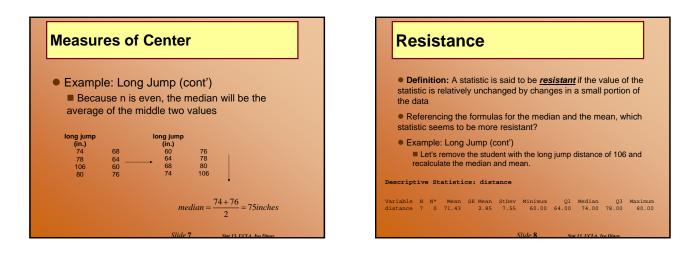
can be thought of as the point that divides a distribution in half (50/50)

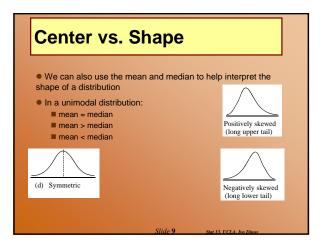
- Steps to find the median:
 - 1. Arrange the data in ascending order $\left(\frac{(n+1)}{2}\right)$

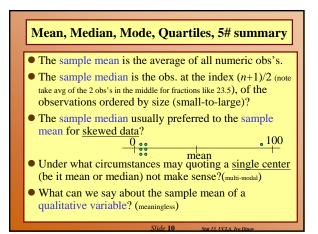
the average of observations $\frac{n}{2}$ and $\left(\frac{n}{2}+1\right)$

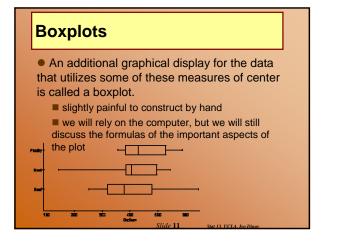
2a. If n is odd, the median is the middle value

2b. If n is even, the median is the average of the middle two values





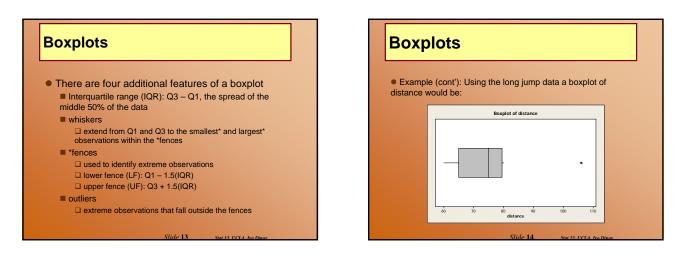


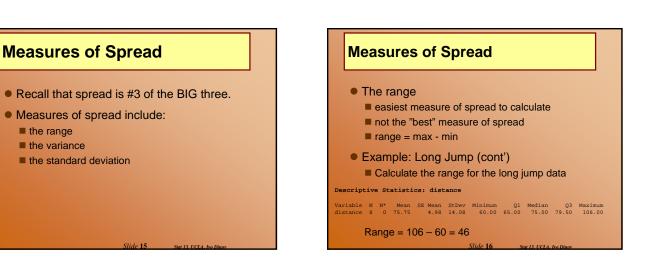


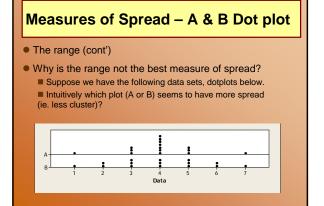
Boxplots

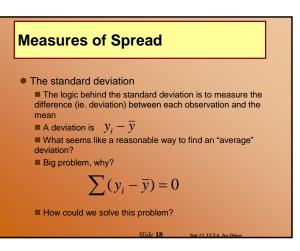
- The five number summary:
 - minimum: the smallest observation
 - maximum: the largest observation
 - median: splits the data into 50/50
 - quartiles: split the data into quarters
 Q1 is the lower quartile and Q3 is the upper quartile

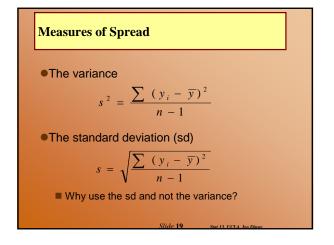
• A boxplot is a visual representation of the five number summary

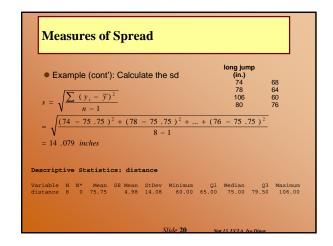


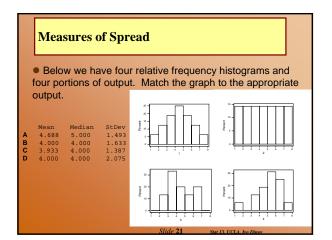












The Empirical Rule

• The empirical rule is useful when talking about a distribution, using the standard deviation in terms of it's distance from the mean.

In general, for symmetric distributions:

 $\overline{y} \pm s \approx 68\%$

 $\overline{y} \pm 2s \approx 95\%$

 $\overline{y} \pm 3s \approx >99\%$

 NOTE: If the distribution is not unimodal symmetric the empirical rule may not hold.

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The Empirical Rule

• Example (hotdogs cont'): From the hotdog data we have the following output:

 Descriptive Statistics: Calories

 Variable
 N N* Mean SE Mean StDev Minimum Q1 Median Q3

 Calories 54
 0 145.44
 4.00
 29.38
 86.00
 131.75
 145.00
 173.50

Variable Maximum Range Calories 195.00 109.00

 $\overline{y} \pm s = 145.44 \pm 29.38 = (116.06,174.82)$

 $\overline{y} \pm 2s = 145.44 \pm 2(29.38) = (86.68,204.20)$

 $\overline{y} \pm 3s = 145.44 \pm 3(29.38) = (57.30,233.58)$

The Empirical Rule • Example (hotdogs Character Stem-and-Leaf Display Stem-and-leaf of Calories N cont'): From the hotdog Leaf Unit = 1.0 data we have the 8 67 following intervals: 9 49 $\overline{y} \pm s = 145.44 \pm 29.38 = (116.06,174.82)$ 9 10 22677 11 11 13 $\overline{y} \pm 2s = 145.44 \pm 2(29.38) = (86.68,204.20)$ 11 11 11 12 12 9 $\overline{y} \pm 3s = 145.44 \pm 3(29.38) = (57.30,233.58)$ 22 13 1225556899 ●30/54 = 55% is this 21 15 223378 15 16 close to 68%? 15 17 235569 9 18 1246 5 19 00015

The Goal

• **Definition:** A *statistical inference* is the process of drawing conclusions about a population based on observations in a sample.

To make a statistical inference we want the sample to be representative of the population.

How could we ensure this?



• **Definition:** *Random* means that each subject of the population must have an equal chance of being selected.

- Why does this seem important for statistics?
- How can we ensure random selection?

