Stat 100a, Introduction to Probability. Rick Paik Schoenberg

Outline for the day:

- 1. Addiction.
- 2. Syllabus, etc.
- 3. Wasicka/Gold/Binger example.
- 4. Meaning of probability.
- 5. Axioms of probability.
- 6. Hw1 terms.
- 7. Basic principle of counting.
- 8. Permutations and combinations.
- 9. R.
- 10. A♠ vs 2♣ after first ace.

2. Syllabus, etc.

For this week:

- (i) Learn the rules of Texas Hold'em. (see http://www.fulltiltpoker.net/holdem.php)
 and http://www.fulltiltpoker.net/handRankHigh.php)
- (ii) Read addiction handout, addiction 1.pdf, on the course website, http://www.stat.ucla.edu/~frederic/100a/S15.
- (iii) Download R and try it out. (http://cran.stat.ucla.edu)
- (iv) Read ch. 1-3 of the textbook.

Note that the CCLE website for this course is not maintained. The course website is http://www.stat.ucla.edu/~frederic/100a/S15.

I do not give hw hints in office hours. Conceptual questions only.

If you have taken Stat 35 before, please see me after class.

Wasicka/Gold/Binger Example

Blinds: \$200,000-\$400,000 with \$50,000 antes.

Chip Counts:

Jamie Gold \$60,000,000 Paul Wasicka \$18,000,000 Michael Binger \$11,000,000

Payouts: 3rd place: \$4,123,310. 2nd place: \$6,102,499. 1st place: \$12,000,000.

Day 7, Hand 229. Gold: 4s 3c. Binger: Ah 10h. Wasicka: 8s 7s.

An example of the type of questions we will be addressing in this class is on the next slide. Don't worry about all the details yet.

Wasicka/Gold/Binger Example, Continued

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Gold: 4 \spadesuit 3 \clubsuit. Binger: A \heartsuit 10 \heartsuit. Wasicka: 8 \spadesuit 7 \spadesuit.
Flop: 10♣ 6♠ 5♠. (Turn: 7♣. River: Q♠.)
                    Wasicka folded?!?
He had 8 \spadesuit 7 \spadesuit and the flop was 10 \clubsuit 6 \spadesuit 5 \spadesuit. Worst case
scenario: suppose he were up against 9 \spadesuit 4 \spadesuit and 9 \heartsuit 9 \spadesuit.
How could Wasicka win?
          88 (3: 8 \clubsuit 8 \blacklozenge, 8 \clubsuit 8 \blacktriangledown, 8 \spadesuit 8 \blacktriangledown)
          77 \qquad (3)
          44 (3)
 [Let "X" = non-49, "Y" = A2378JQK, and "n" = non-\spadesuit.]
          4n Xn (3 x 32)
          9♣ 4n (3)
          9 Yn (24). Total: 132 out of 903 = 14.62\%.
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4. Meaning of Probability.

Notation: "P(A) = 60%". A is an *event*. Not "P(60%)".

Definition of probability:

Frequentist: If repeated independently under the same conditions millions and millions of times, A would happen 60% of the times.

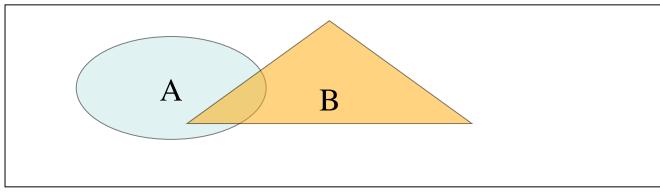
Bayesian: Subjective feeling about how likely something seems.

P(A or B) means P(A or B or both) Mutually exclusive: P(A and B) = 0. Independent: P(A given B) [written "P(A|B)"] = P(A). $P(A^c)$ means P(not A).

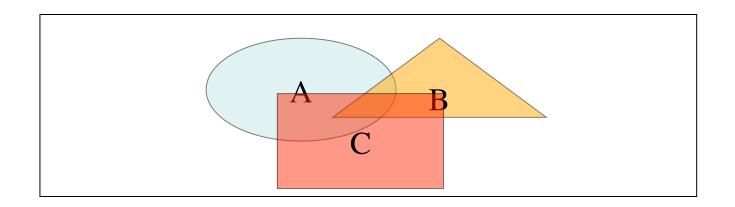
5. Axioms (initial assumptions/rules) of probability:

- 1) $P(A) \ge 0$.
- 2) $P(A) + P(A^c) = 1$.
- 3) If A_1, A_2, A_3, \dots are mutually exclusive, then $P(A_1 \text{ or } A_2 \text{ or } A_3 \text{ or } \dots) = P(A_1) + P(A_2) + P(A_3) + \dots$

(#3 is sometimes called the *addition rule*)
Probability <=> Area. Measure theory, Venn diagrams



P(A or B) = P(A) + P(B) - P(A and B).



Fact: P(A or B) = P(A) + P(B) - P(A and B). P(A or B or C) = P(A) + P(B) + P(C) - P(AB) - P(AC) - P(BC) + P(ABC).

Fact: If $A_1, A_2, ..., A_n$ are equally likely & mutually exclusive, and if $P(A_1 \text{ or } A_2 \text{ or } ... \text{ or } A_n) = 1$, then $P(A_k) = 1/n$.

[So, you can *count*: $P(A_1 \text{ or } A_2 \text{ or } \dots \text{ or } A_k) = k/n.$]

Ex. You have 76, and the board is KQ54. P(straight)? [52-2-4=46.] P(straight) = P(8 on river OR 3 on river) = P(8 on river) + P(3 on river) = 4/46 + 4/46. **6. Hw1 terms.** flop a flush, the nuts, pocket pair.

Let me explain a bit what I mean on 2.18.

Suppose the board is $\mathbb{K}^{\blacktriangledown} \mathbb{Q} \triangleq 10 \mathbb{V} = 6 \triangleq 3 \triangleq 10$ and you have $\mathbb{A}^{\blacktriangledown} \mathbb{J} \triangleq 10$. Then you have the nuts, and your 5-card hand is an ace-high straight (AKQJ10). Suppose instead that the board is $\mathbb{K}^{\blacktriangledown} \mathbb{Q} \triangleq 7 \mathbb{V} = 6 \triangleq 3 \triangleq 10$. Then if you have $\mathbb{S}^{\blacktriangledown} = 4 \triangleq 10$ you have the nuts, and your 5-card hand is a 7-high straight (76543). A 7-high straight is *worse* than an ace-high straight, in the sense that it is outranked by an ace-high straight in the hand rankings. Now, if the board is $\mathbb{K}^{\blacktriangledown} = 10 \triangleq 10 \triangleq 10 \triangleq 10 \triangleq 10$, and you have $\mathbb{K}^{\clubsuit} = 10 \triangleq 10 \triangleq 10$, which is a worse hand than a 7-high straight. This question is asking: how far can you go with this? Can you think of a different board, so that it is possible that the nuts is a 5-card hand even worse than $\mathbb{K} = 10 \triangleq 10 \triangleq 10$. What is the worst possible?

7. Basic Principle of Counting.

If there are a_1 distinct possible outcomes on experiment #1, and for each of them, there are a_2 distinct possible outcomes on experiment #2, then there are $a_1 \times a_2$ distinct possible *ordered* outcomes on both.

e.g. you get 1 card, opp. gets 1 card. # of distinct possibilities? 52×51 . [ordered: $(A \clubsuit, K \heartsuit) \neq (K \heartsuit, A \clubsuit)$.]

In general, with j experiments, each with a_i possibilities, the # of distinct outcomes where order matters is $a_1 \times a_2 \times ... \times a_i$.

8. Permutations and Combinations.

e.g. you get 1 card, opp. gets 1 card.

of distinct possibilities?

52 x 51. [ordered: $(A \clubsuit, K \lor) \neq (K \lor, A \clubsuit)$.]

Each such outcome, where order matters, is called a *permutation*.

Number of permutations of the deck? $52 \times 51 \times ... \times 1 = 52!$

$$\sim 8.1 \times 10^{67}$$

A <u>combination</u> is a collection of outcomes, where order <u>doesn't</u> matter.

e.g. in hold'em, how many distinct 2-card hands are possible?

52 x 51 if order matters, but then you'd be double-counting each

[since now
$$(A \clubsuit, K \heartsuit) = (K \heartsuit, A \clubsuit)$$
.]

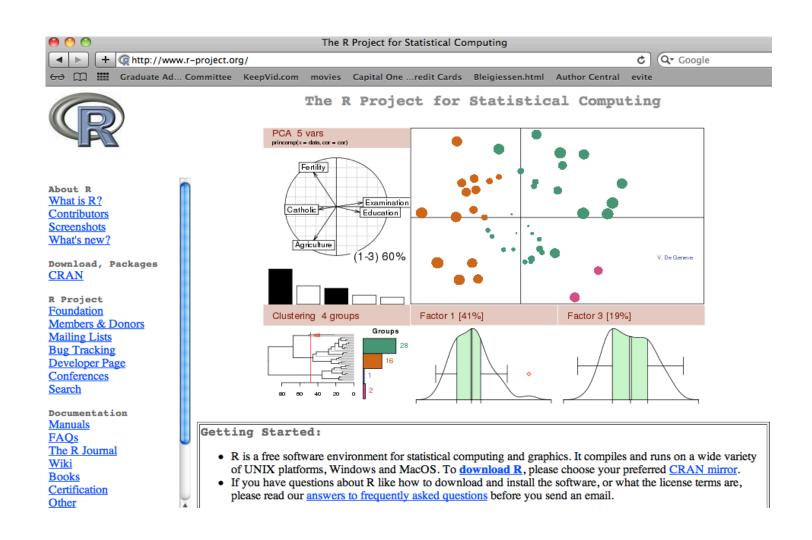
So, the number of *distinct* hands where *order doesn't matter* is $52 \times 51 / 2$.

In general, with n distinct objects, the # of ways to choose k *different* ones, where order doesn't matter, is

"n choose k" = choose(n,k) =
$$\underline{n!}$$
.

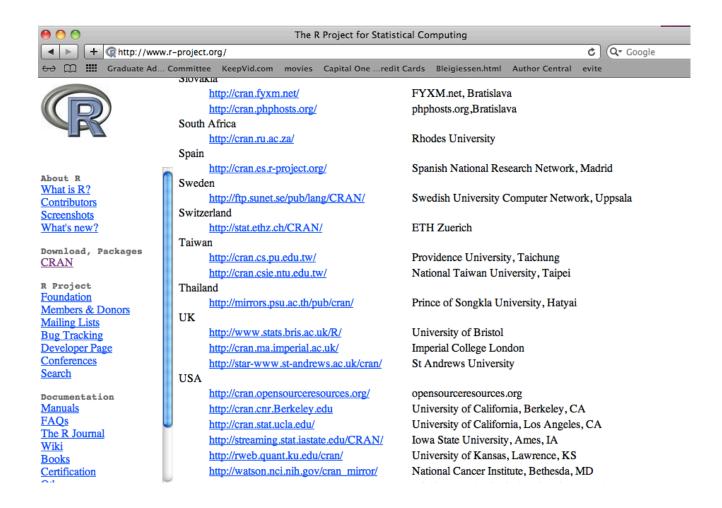
k! (n-k)!

9. R. To download and install R, go directly to cran.stat.ucla.edu, or as it says in the book at the bottom of p157, you can start at www.r-project.org, in which case you click on "download R", scroll down to UCLA, and click on cran.stat.ucla.edu. From there, click on "download R for ...", and then get the latest version.

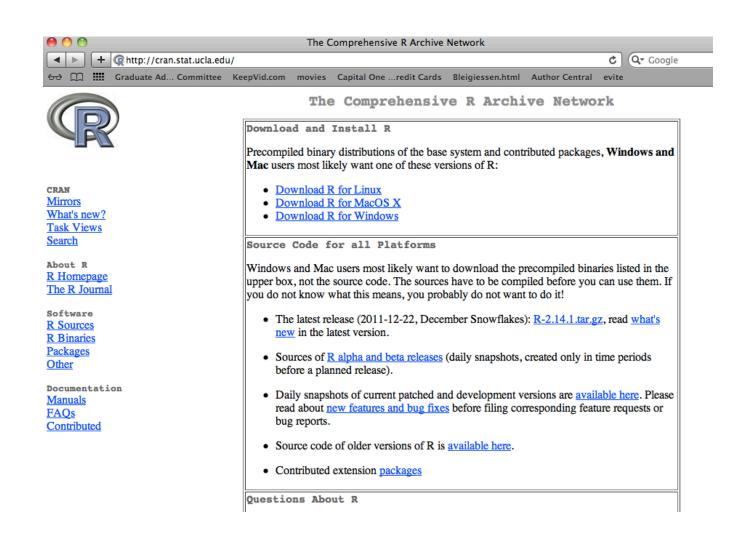


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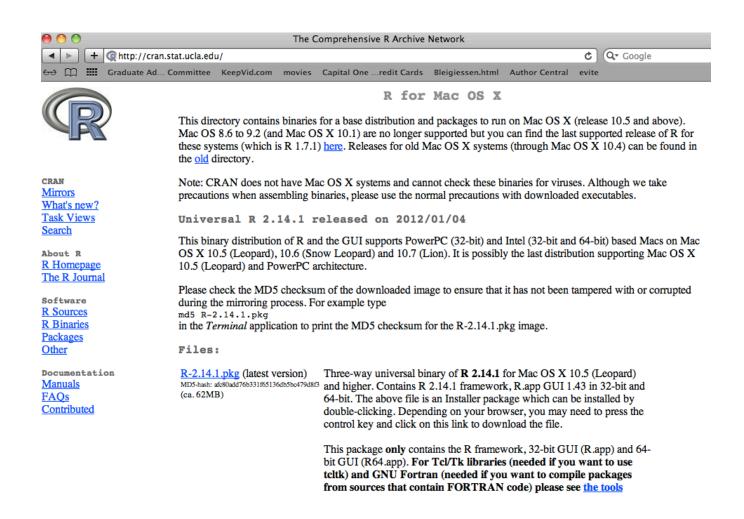
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10. Deal til first ace appears. Let $X = the \ next$ card after the ace.

$$P(X = A - ?)? P(X = 2 - ?)?$$