Stat 13, Intro. to Statistical Methods for the Life and Health Sciences.

- 1. When to use which formula.
- 2. Review list.
- 3. Example problems.

Read ch6. The midterm will be on ch 1-6.

http://www.stat.ucla.edu/~frederic/13/W23.

Bring a PENCIL and CALCULATOR and any books or notes you want to the midterm and final. You cannot use a computer, laptop, ipad, or phone on the exams though.

No class Mon Feb20, President's Day!

## t versus normal and assumptions.

Suppose  $X_1, ..., X_n$  are iid with mean  $\mu$  and SD  $\sigma$ .

CLT:  $(\bar{x} - \mu) \div (\sigma/\sqrt{n}) \sim \text{std. normal.}$ 

If  $X_1, ..., X_n$  are normal, then  $(\bar{x} - \mu) \div (\sigma/\sqrt{n})$  is std. normal.

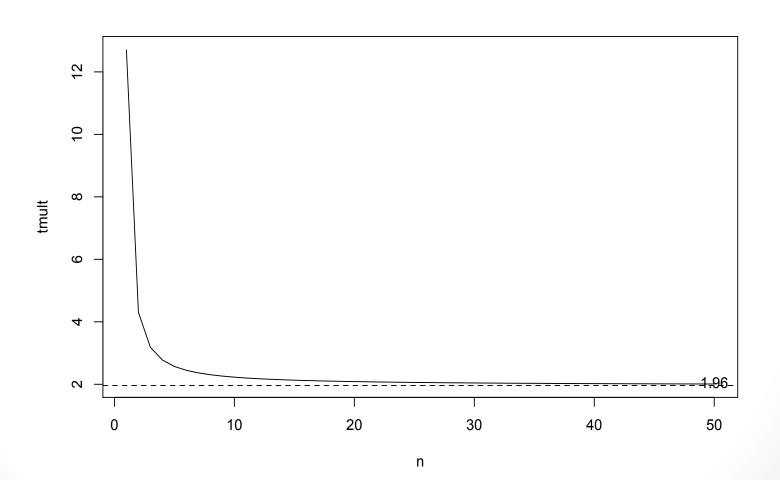
 $\sigma$  is the SD of the population from which  $X_1, ..., X_n$  are drawn. s is the SD of the sample,  $X_1, ..., X_n$ .

Gosset (1908) showed that replacing  $\sigma$  with s, if  $X_1, ..., X_n$  are normal, then  $(\bar{x} - \mu) \div (s/vn)$  is t distributed. So we need the multiplier from the t distribution.

## t versus normal and assumptions.

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To sum up,
if the observations are iid and n is large, then
       P(\mu is in the range \bar{x} +/- 1.96 \sigma/\nun) ~ 95%.
If the observations are iid and normal, then
       P(\mu is in the range \bar{x} +/- 1.96 \sigma/\nun) ~ 95%.
If the obs. are iid and normal and \sigma is unknown, then
       P(\mu is in the range \bar{x} +/- t_{mult} s/\foralln) ~ 95%.
where t_{mult} is the multiplier from the t distribution.
This multiplier depends on n.
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# t versus normal and assumptions.



- a. 1 sample numerical data, iid observations, want a 95% CI for  $\mu$ .
- If n is large and  $\sigma$  is known, use  $\bar{x}$  +/- 1.96  $\sigma/\sqrt{n}$ .
- If n is small, draws are normal, and  $\sigma$  is known, use  $\bar{x}$  +/- 1.96  $\sigma/\sqrt{n}$ .
- If n is small, draws are normal, and  $\sigma$  is unknown, use  $\bar{x}$  +/-  $t_{mult}$  s/ $\sqrt{n}$ .
- If n is large and  $\sigma$  is unknown,  $t_{mult} \sim 1.96$ , so we can use  $\bar{x}$  +/- 1.96 s/vn.

 $n \ge 30$  is often considered large enough to use 1.96.

In practice, we typically do not know the draws are normal, but if the distribution looks roughly symmetrical without enormous outliers, the t formula may be reasonable.

b. 1 sample binary data, iid observations, want a 95% CI for  $\pi$ .

View the data as 0 or 1, so sample percentage  $p = \bar{x}$ , and  $s = \sqrt{[p(1-p)]}$ ,  $\sigma = \sqrt{[\pi(1-\pi)]}$ .

- a. 1 sample numerical data, iid observations, want a 95% CI for μ.
- If n is large and  $\sigma$  is known, use  $\bar{x}$  +/- 1.96  $\sigma/\sqrt{n}$ .
- If n is small, draws are normal, and  $\sigma$  is known, use  $\bar{x}$  +/- 1.96  $\sigma/\sqrt{n}$ .
- If n is small, draws ~ normal, and  $\sigma$  is unknown, use  $\bar{x}$  +/-  $t_{mult}$  s/ $\sqrt{n}$ .
- If n is large and  $\sigma$  is unknown,  $t_{\text{mult}} \sim 1.96$ , so we can use  $\bar{x}$  +/- 1.96 s/vn.
- b. 1 sample binary data, iid observations, want a 95% CI for  $\pi$ .

View the data as 0 or 1, so sample percentage  $p = \overline{x}$ , and

$$s = V[p(1-p)], \sigma = \sqrt{[\pi(1-\pi)]}.$$

If n is large and  $\pi$  is unknown, use  $\overline{x}$  +/- 1.96 s/ $\sqrt{n}$ .

Here large n means ≥ 10 of each type in the sample.

What if n is small and the draws are not normal, and you want a theory-based test or CI?

How should you find the t multiplier for a CI or a p-value using the t-statistic, when n is small?

These are questions outside the scope of this course, but some techniques have been developed, such as the bootstrap, which are sometimes useful in these situations.

c. Numerical data from 2 samples, iid observations, want a 95% CI for  $\mu_1$  -  $\mu_2$ .

If n is large and 
$$\sigma$$
 is unknown, use  $\bar{x_1}$  -  $\bar{x_2}$ +/- 1.96  $\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$ .

As with one sample, if  $\sigma_1$  is known, replace  $s_1$  with  $\sigma_1$ , and the same for  $\sigma_2$ . And as with one sample, if  $\sigma_1$  and  $\sigma_2$  are unknown, the sample sizes are small, and the distributions are roughly normal, then use  $t_{mult}$  instead of 1.96. If the sample sizes are small, the distributions are normal, and  $\sigma_1$  and  $\sigma_2$  are known, then use 1.96.

d. Binary data from 2 samples, iid observations, want a 95% CI for  $\pi_1$  -  $\pi_2$ .

same as in c above, with  $p_1 = \overline{x_1}$ ,  $s_1 = \sqrt{[p_1(1-p_1)]}$ ,  $\sigma_1 = \sqrt{[\pi_1(1-\pi_1)]}$ .

Large for binary data means sample has ≥ 10 of each type.

For testing, use pooled estimate of p for the SE.

For CIs for the difference in proportions,

SE = 
$$\sqrt{\left(\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}\right)}$$

In testing the difference in proportions,

$$\mathsf{SE} = \sqrt{\left(\frac{\hat{p}(1-\hat{p})}{n_1} + \frac{\hat{p}(1-\hat{p})}{n_2}\right)}$$

where  $\hat{p}$  is the proportion in both groups combined.

#### 2. Review list.

- 1. Meaning of SD.
- 2. Parameters and statistics.
- 3. Z statistic for proportions.
- 4. Simulation and meaning of pvalues.
- 5. SE for proportions.
- 6. What influences pvalues.
- 7. CLT and validity conditions for tests.
- 8. 1-sided and 2-sided tests.
- 9. Reject the null vs. accept the alternative.
- 10. Sampling and bias.
- 11. Significance level.
- 12. Type I, type II errors, and power.
- 13. Cls for a proportion.
- 14. Cls for a mean.
- 15. Margin of error.
- 16. Practical significance.
- 17. Confounding.
- 18. Observational studies and experiments.

- 19. Random sampling and random assignment.
- 20. Two proportion CIs and testing.
- 21. IQR and 5 number summaries.
- 22. Testing and CIs for 2 means.
- 23. Placebo effect, adherer bias, and nonresponse bias.
- 24. Prediction and causation.

## 3. Example problems.

NCIS was the top-rated tv show in 2014. It was 3<sup>rd</sup> in 2016 and is now 5<sup>th</sup> in 2017.

A study finds that in a certain city, people who watch NCIS are much more likely to die than people who do not watch NCIS. Can we conclude that NCIS is a dangerous tv show to watch?

# Example problems.

NCIS was the top-rated tv show in 2022.

A study finds that in a certain city, people who watch NCIS are much more likely to die than people who do not watch NCIS. Can we conclude that NCIS is a dangerous tv show to watch?

No. Age is a confounding factor. The median age of a viewer is 61 years old.

- 1. Suppose the population of American adults has a mean systolic blood pressure of 120 mm Hg and an SD of 20 mm Hg.
   You take a simple random sample of 100 American adults.
   Which of the following is true?
- A typical adult's blood pressure would differ from 120 by about 20 mm Hg, and a typical sample of size 100 would have a sample mean that differs from 120 by about 2 mm Hg.
- A typical adult's blood pressure would differ from 120 by about 20 mm Hg, and a typical sample of size 100 would have a sample mean that differs from 120 by about 20 mm Hg.
- A typical adult's blood pressure would differ from 120 by about 2 mm Hg, and a typical sample of size 100 would have a sample mean that differs from 120 by about 0.2 mm Hg.
- A typical adult's blood pressure would differ from 120 by about 20 mm Hg, and a typical sample of size 100 would have a sample mean that differs from 120 by about 0.2 mm Hg.

- 1. Suppose the population of American adults has a mean systolic blood pressure of 120 mm Hg and an SD of 20 mm Hg.
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- A typical adult's blood pressure would differ from 120 by about **20** mm Hg, and a typical sample of size 100 would have a sample mean that differs from 120 by about **20** mm Hg.
- A typical adult's blood pressure would differ from 120 by about
   2 mm Hg, and a typical sample of size 100 would have a sample mean that differs from 120 by about 0.2 mm Hg.
- A typical adult's blood pressure would differ from 120 by about **20** mm Hg, and a typical sample of size 100 would have a sample mean that differs from 120 by about **0.2** mm Hg.