

# Stat 13, Intro. to Statistical Methods for the Life and Health Sciences.

1. Exams back and announcements.
2. Finish up theory based approach for paired data and M&M example.
3. Multiple testing and publication bias.
4. Two quantitative variables, scatterplot and correlation.
5. Inference for correlation using simulations.

There will be no lecture or OH Mon Mar11.

Read ch7 and 10.

Hw4 is due Mon Mar11 1159pm by email to statgrader or statgrader2.

10.1.8, 10.3.14, 10.3.21, and 10.4.11.

<http://www.stat.ucla.edu/~frederic/13/W24> .

**If you are in Section 2c or 2d, please resubmit your hw1 to statgrader2@stat.ucla.edu by tonight, Mon, Mar4, 1159pm.**

For the final exam, bring a pencil or pen, and a calculator. On the final exam, you cannot use computers or ipads or phones or anything that can surf the web or do email.

**10.1.8** Which of the following statements is correct?

- A.** Changing the units of measurements of the explanatory or response variable does not change the value of the correlation.
- B.** A negative value for the correlation indicates that there is no relationship between the two variables.
- C.** The correlation has the same units (e.g., feet or minutes) as the explanatory variable.
- D.** Correlation between  $y$  and  $x$  has the same number but opposite sign as the correlation between  $x$  and  $y$ .

## 10.3.14.

**10.3.12** Reconsider the previous five exercises and the Legos data file. The last product listed in the data file has 415 pieces and a price of \$49.99.

- Determine the predicted price for such a product.
- Determine the residual value for this product.
- Interpret what this residual value means.
- Does the product fall above or below the least squares line in the graph? Explain how you can tell, based on its residual value.

**10.3.13** Reconsider the previous six exercises and the Legos data file. This is very unrealistic, but suppose that one of the products were to be offered at a price of \$0.

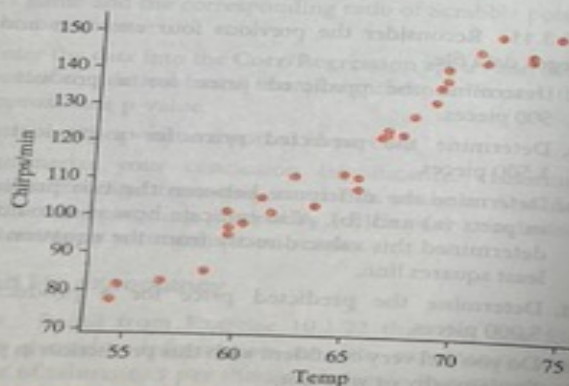
- Would you expect this change to affect the least squares line very much? Explain.
- For which one product would you expect this change to have the greatest impact on the least squares line? Explain how you choose this product.
- Change the price to \$0 for the product that you identified in part (b). Report the (new) equation of the least squares line and the (new) value of  $r^2$ . Have these values changed considerably?

### Crickets

**10.3.14** Consider the following two scatterplots based on data gathered in a study of 30 crickets, with temperature measured in degrees Fahrenheit and chirp frequency measured in chirps per minute.

- If the goal is to predict temperature based on a cricket's chirps per minute, which is the appropriate scatterplot to examine—the one on the left or the one on the right? Explain briefly.

One of the following is the correct equation of the least squares line for predicting temperature from chirps per minute:



EXERCISE 10.3.14

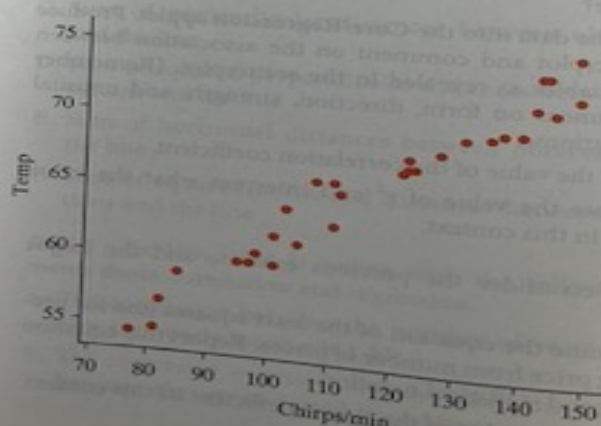
- predicted temperature =  $35.78 + 0.25$  chirps per minute
- predicted temperature =  $-131.23 + 3.81$  chirps per minute
- predicted temperature =  $83.54 - 0.25$  chirps per minute

- Which is the correct equation? Circle your answer and explain briefly.
- Use the correct equation to predict the temperature when the cricket is chirping at 100 chirps per minute.
- Interpret the value of the slope coefficient, in this context, for whichever equation you think is the correct one.

### Cat jumping\*

**10.3.15** Harris and Steudel (2002) studied factors that might be associated with the jumping performance of domestic cats. They studied 18 cats, using takeoff velocity (in centimeters per second) as the response variable. They used body mass (in grams), hind limb length (in centimeters), muscle mass (in grams), and percent body fat in addition to sex as potential explanatory variables. The data can be found in the CatJumping data file. A scatterplot of takeoff velocity vs. body mass is shown in the figure for Exercise 10.3.15.

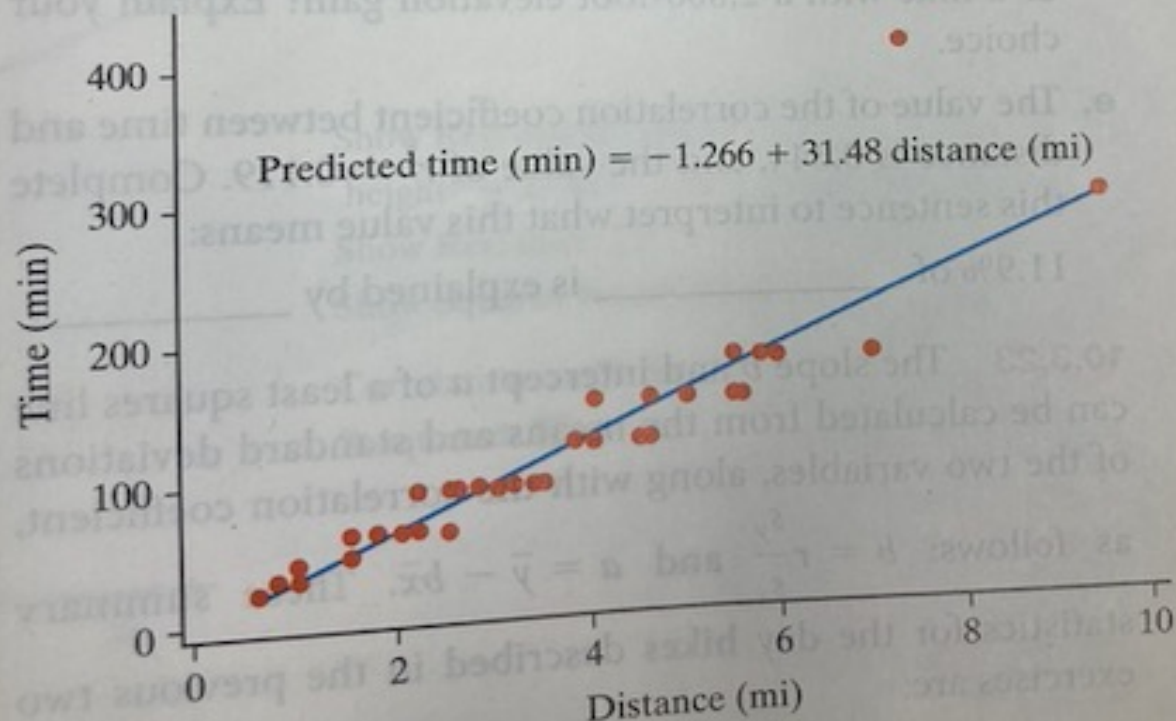
- Describe the association between these variables.
- Use the **Corr/Regression** applet to determine the equation of the least squares line for predicting a cat's takeoff velocity from its mass.
- Interpret the value of the slope coefficient in this context.
- Interpret the value of the intercept coefficient. Is this a context in which the intercept coefficient is meaningful?
- Determine the proportion of variability in takeoff velocity that is explained by the least squares line with mass.



10.3.21.

### Day hikes

**10.3.21** The book *Day Hikes in San Luis Obispo County* lists information about 72 hikes, including the distance of the hike (in miles), the elevation gain of the hike (in feet), and the time that the hike is expected to take (in minutes). Consider the scatterplot below, with least squares regression line superimposed:





- a. Report the value of the slope coefficient for predicting time from distance.
- b. Write a sentence interpreting the value of the slope coefficient for predicting time from distance.
- c. Use the line to predict how long a 4-mile hike will take.
- d. Would you feel more comfortable using the line predict the time for a 4-mile hike or for a 12-mile hike? Explain your choice.
- e. The value of the correlation coefficient between time and distance is 0.916, and the value of  $r^2 = 0.839$ . Complete this sentence to interpret what this value means:  
83.9% of \_\_\_\_\_ is explained by \_\_\_\_\_.

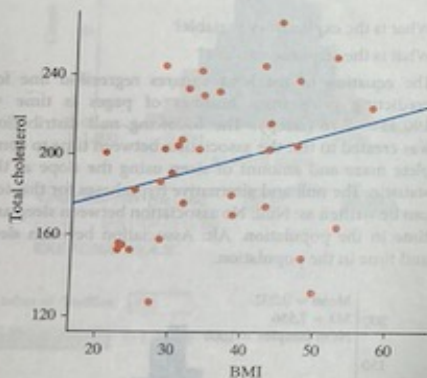
**10.3.22** Reconsider the previous exercise. The following

**10.4.10** Reconsider the previous exercise about the amount of sleep (in hours) obtained in the previous night and time to complete a paper and pencil maze (in seconds). The equation of the least squares regression line for predicting price from number of pages is  $\text{time} = 190.33 - 7.76 (\text{sleep})$ .

- Interpret what the slope coefficient means in the context of sleep and time to complete the maze.
- Interpret the intercept. Is this an example of extrapolation? Why or why not?

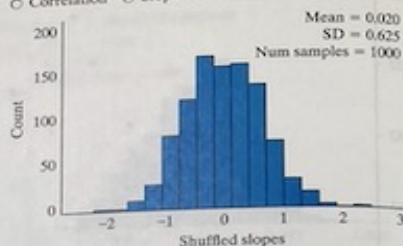
#### Weight loss and protein

**10.4.11** In a study to see if there was an association between weight loss and the amount of a certain protein in a person's body fat, the researchers measured a number of different attributes in their 39 subjects at the beginning of the study. The article reported, "These subjects were clinically and ethnically heterogeneous." Two of the variables they measured were body mass index (BMI) and total cholesterol. The results are shown in the scatterplot along with the regression line.



- What are the observational units in the study?
- The equation of the least squares regression line for predicting total cholesterol from BMI is  $\text{cholesterol} = 162.56 + 0.9658 (\text{BMI})$ . The following null distribution was created to test the association between people's total cholesterol number and their BMI using the slope as the statistic. The null and alternative hypotheses for this test can be written as: Null: No association between cholesterol and BMI in the population. Alt: Association between cholesterol and BMI in the population.

○ Correlation ○ Slope ○ t-statistic



- Based on information shown in the null distribution, how many standard deviations is our observed statistic below the mean of the null distribution? (That is, what is the standardized statistic?)
- Based on your standardized statistic, do you have strong evidence of an association between a people's total cholesterol and their BMI? Explain.

**10.4.12** Reconsider the previous exercise about the cholesterol and BMI. The equation of the least squares regression line obtained was  $\text{cholesterol} = 162.56 + 0.9658 (\text{BMI})$ .

- Interpret what the slope coefficient means in the context of cholesterol and BMI.
- Interpret the intercept. Is this an example of extrapolation? Why or why not?

#### Honda Civic prices\*

**10.4.13** The data in the file **UsedHondaCivics** come from a sample of used Honda Civics listed for sale online in July 2006. The variables recorded are the car's age (calculated as 2006 minus year of manufacture) and price. Consider conducting a simulation analysis to test whether the sample data provide strong evidence of an association between a car's price and age in the population in terms of the population slope.

- State the appropriate null and alternative hypotheses.
- Conduct a simulation analysis with 1,000 repetitions. Describe how to find your p-value from your simulation results and report this p-value.
- Summarize your conclusion from this simulation analysis. Also describe the reasoning process by which your conclusion follows from your simulation results.

**10.4.14** Reconsider the previous exercise on prices of Honda Civics.

- Find the regression equation that predicts the price of the car given its age.
- Interpret the slope and intercept of the regression line.

# Conclusion

- The theory-based test gives slightly different results than simulation, 11.7% instead of 12.2% for the p-value, but we come to the same conclusion. We do not have strong evidence that the bowl size affects the number of M&Ms taken.
- We can see this in the large p-value (0.1172) and the confidence interval that included zero (-29.5, 7.8).
- The confidence interval tells us that we are 95% confident that when given a small bowl, people will take somewhere between 29.5 fewer M&Ms to 7.8 more M&Ms on average than when given a large bowl.

# Why wasn't the difference statistically significant?

- There could be a number of reasons we didn't get significant results.
  - Maybe bowl size doesn't matter.
  - Maybe bowl size does matter and the difference was too small to detect with our small sample size.
  - Maybe bowl size does matter with some foods, like pasta or cereal, but not with a snack food like M&Ms.



# Strength of Evidence

- We will have stronger evidence against the null (smaller p-value) when:
  - The sample size is increased.
  - The variability of the data is reduced.
  - The effect size, or mean difference, is farther from 0.
- We will get a narrower confidence interval when:
  - The sample size is increased.
  - The variability of the data is reduced.
  - The confidence level is decreased.

### 3. Multiple testing and publication bias.

A p-value is the probability, assuming the null hypothesis of no relationship is true, that you will see a difference as extreme as, or more extreme than, you observed.

So, when you are looking at unrelated things, 5% of the time you will find a statistically significant relationship.

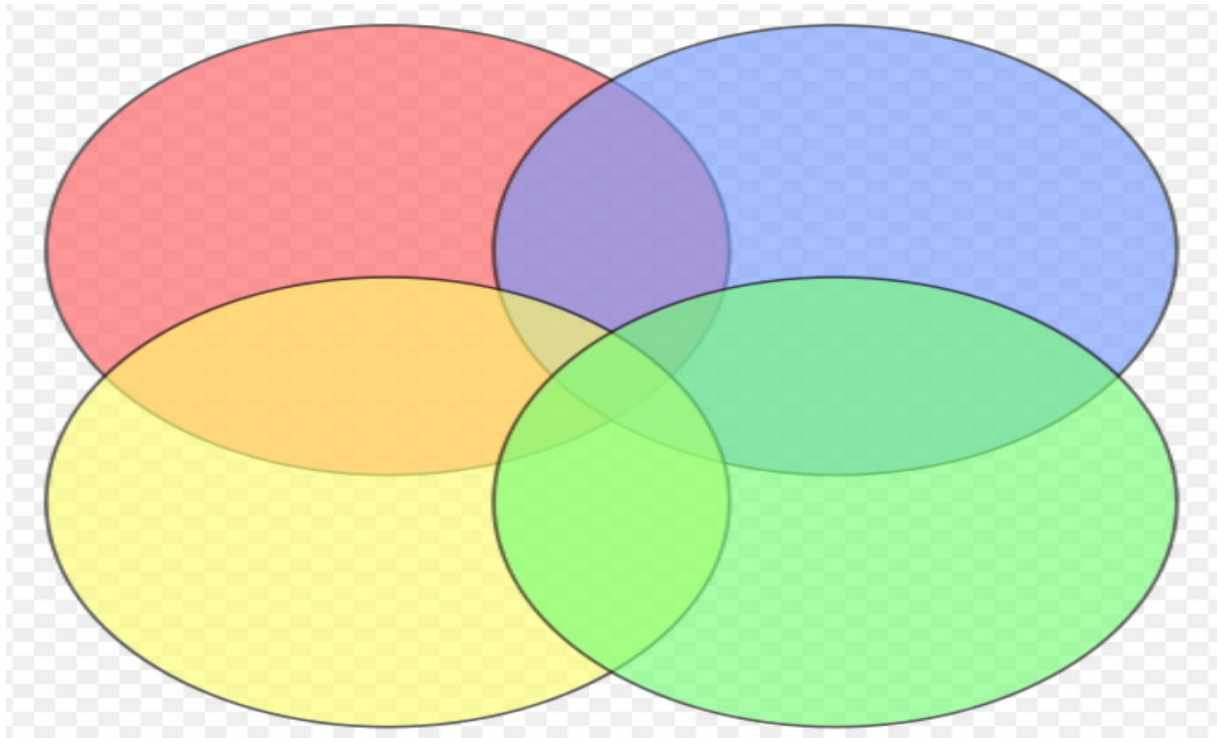
This underscores the need for followup confirmation studies. If testing many explanatory variables simultaneously, it can become very likely to find something significant even if nothing is actually related to the response variable.

# Multiple testing and publication bias.

- \* For example, if the significance level is 5%, then for 100 tests where all null hypotheses are true, the expected number of incorrect rejections (Type I errors) is 5. If the tests are independent, the probability of at least one Type I error would be 99.4%.  $P(\text{no Type I errors}) = .95^{100} = 0.6\%$ .

- \* To address this problem, scientists sometimes change the significance level so that, under the null hypothesis that none of the explanatory variables is related to the response variable, the probability of rejecting at least one of them is 5%.

- \* One way is to use Bonferroni's correction: with  $m$  explanatory variables, use significance level  $5\%/m$ .  $P(\text{at least 1 Type I error}) \text{ will be } \leq m (5\%/m) = 5\%$ .



$P(\text{Type I error on explanatory 1}) = 5\%/m.$

$P(\text{Type I error on explanatory 2}) = 5\%/m.$

$P(\text{Type 1 error on at least one explanatory}) \leq$

$P(\text{error on 1}) + P(\text{error on 2}) + \dots + P(\text{error on } m) = m \times 5\%/m.$



# Multiple testing and publication bias.

Imagine a scenario where a drug is tested many times to see if it reduces the incidence of some response variable. If the drug is tested 100 times by 100 different researchers, the results will be stat. sig. about 5 times.

If only the stat. sig. results are published, then the published record will be very misleading.

# Multiple testing and publication bias.

A drug called Reboxetine made by Pfizer was approved as a treatment for depression in Europe and the UK in 2001, based on positive trials.

A meta-analysis in 2010 found that it was not only ineffective but also potentially harmful. The report found that 74% of the data on patients who took part in the trials of Reboxetine were not published because the findings were negative. Published data about reboxetine overestimated its benefits and underestimated its harm.

A subsequent 2011 analysis indicated Reboxetine might be effective for severe depression though.

# 4. Two quantitative variables.

Chapter 10

# Two Quantitative Variables: Scatterplots and Correlation

Section 10.1



# Scatterplots and Correlation

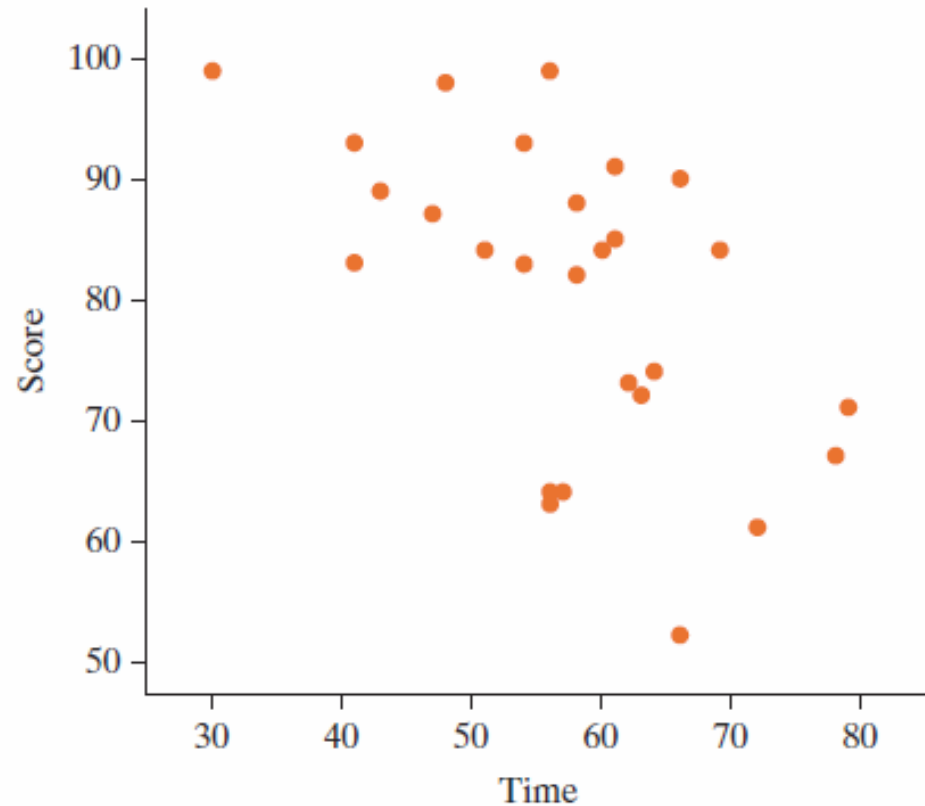
Suppose we collected data on the relationship between the time it takes a student to take a test and the resulting score.

<b>Time</b>	30	41	41	43	47	48	51	54	54	56	56	56	57	58
<b>Score</b>	100	84	94	90	88	99	85	84	94	100	65	64	65	89
<b>Time</b>	58	60	61	61	62	63	64	66	66	69	72	78	79	
<b>Score</b>	83	85	86	92	74	73	75	53	91	85	62	68	72	

# Scatterplot

Put explanatory variable on the horizontal axis.

Put response variable on the vertical axis.



# Describing Scatterplots

- When we describe data in a scatterplot, we describe the
  - Direction (positive or negative)
  - Form (linear or not)
  - Strength (strong-moderate-weak, we will let correlation help us decide)
  - Unusual Observations
- How would you describe the time and test scatterplot?

# Correlation

- **Correlation** measures the strength and direction of a linear association between two quantitative variables.
- Correlation is a number between -1 and 1.
- With positive correlation one variable increases, on average, as the other increases.
- With negative correlation one variable decreases, on average, as the other increases.
- The closer it is to either -1 or 1 the closer the points fit to a line.
- The correlation for the test data is -0.56.



# Correlation Guidelines

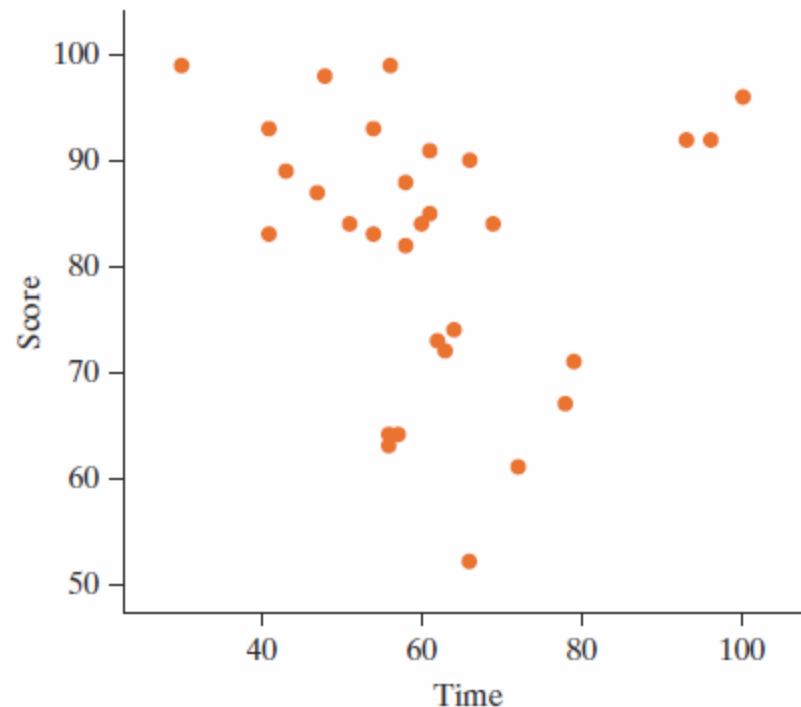
Correlation Value	Strength of Association	What this means
0.7 to 1.0	Strong	The points will appear to be nearly a straight line
0.3 to 0.7	Moderate	When looking at the graph the increasing/decreasing pattern will be clear, but there is considerable scatter.
0.1 to 0.3	Weak	With some effort you will be able to see a slightly increasing/decreasing pattern
0 to 0.1	None	No discernible increasing/decreasing pattern

Same Strength Results with Negative Correlations

# Back to the test data

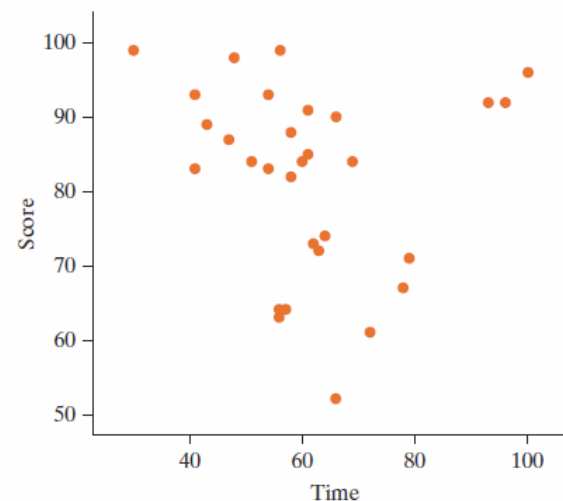
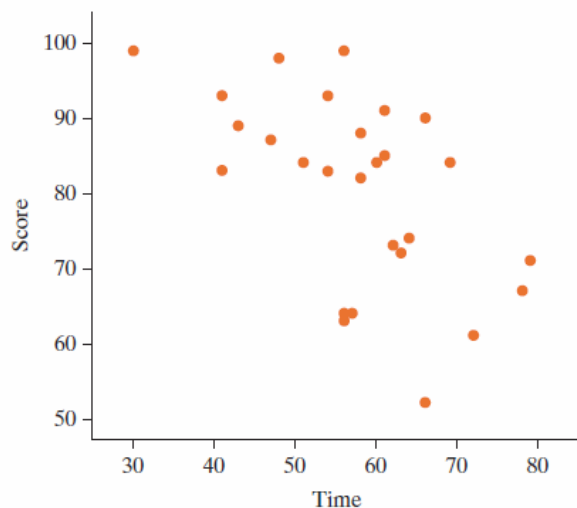
Actually the last three people to finish the test had scores of 93, 93, and 97.

What does this do  
to the correlation?



# Influential Observations

- The correlation changed from -0.56 (a fairly moderate negative correlation) to -0.12 (a weak negative correlation).
- Points that are far to the left or right and not in the overall direction of the scatterplot can greatly change the correlation. (influential observations)



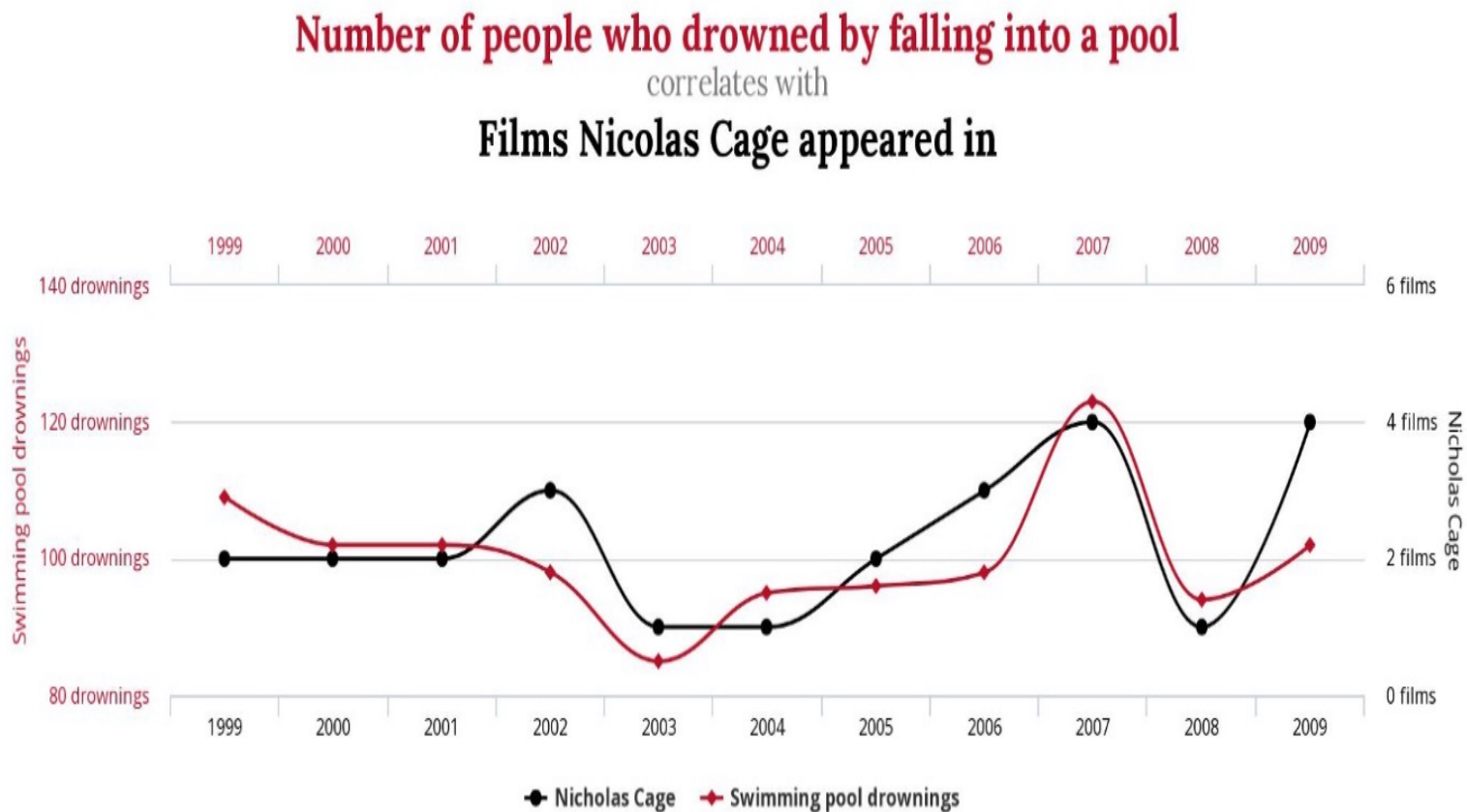
# Correlation

- **Correlation** measures the strength and direction of a linear association between two quantitative variables.
  - $-1 \leq r \leq 1$
  - Correlation makes no distinction between explanatory and response variables.
  - Correlation has no units.
  - Correlation is not resistant to outliers. It is sensitive.

# Learning Objectives for Section 10.1

- Summarize the characteristics of a scatterplot by describing its direction, form, strength and whether there are any unusual observations.
- Recognize that the correlation coefficient is appropriate only for summarizing the strength and direction of a scatterplot that has linear form.
- Recognize that a scatterplot is the appropriate graph for displaying the relationship between two quantitative variables and create a scatterplot from raw data.
- Recognize that a correlation coefficient of 0 means there is no linear association between the two variables and that a correlation coefficient of -1 or 1 means that the scatterplot is exactly a straight line.
- Understand that the correlation coefficient is influenced by extreme observations.

# Note that correlation $\neq$ causation.



tylervigen.com

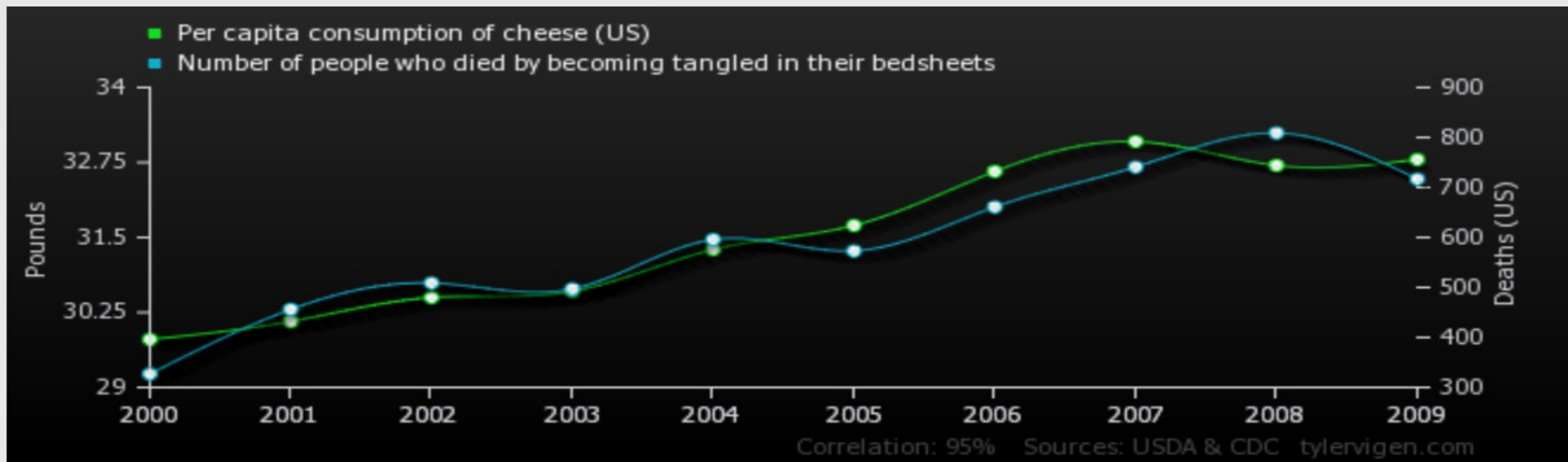
from: <http://tylervigen.com>

# Note that correlation $\neq$ causation.

## Per capita consumption of cheese (US)

correlates with

## Number of people who died by becoming tangled in their bedsheets

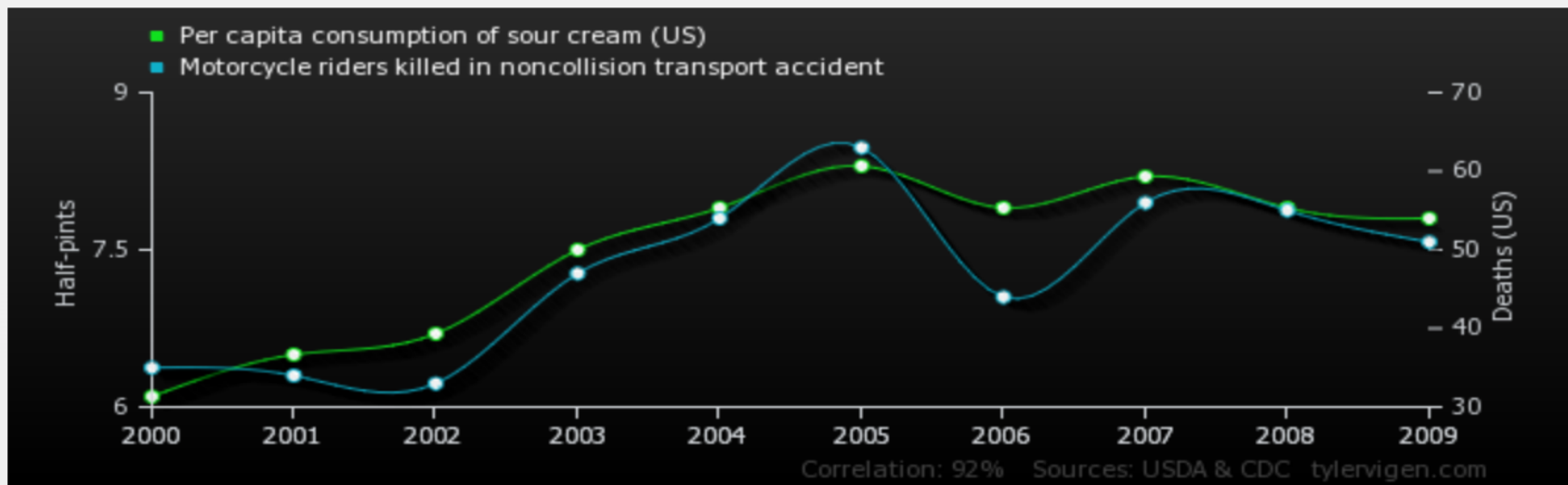


	2000	2001	2002	2003	2004	2005	2006	2007	2008	2009
Per capita consumption of cheese (US) Pounds (USDA)	29.8	30.1	30.5	30.6	31.3	31.7	32.6	33.1	32.7	32.8
Number of people who died by becoming tangled in their bedsheets Deaths (US) (CDC)	327	456	509	497	596	573	661	741	809	717

Correlation: 0.947091

# Note that correlation $\neq$ causation.

## Per capita consumption of sour cream (US) correlates with Motorcycle riders killed in noncollision transport accident



	2000	2001	2002	2003	2004	2005	2006	2007	2008	2009
Per capita consumption of sour cream (US) Half-pints (USDA)	6.1	6.5	6.7	7.5	7.9	8.3	7.9	8.2	7.9	7.8
Motorcycle riders killed in noncollision transport accident Deaths (US) (CDC)	35	34	33	47	54	63	44	56	55	51

Correlation: 0.916391



# Inference for the Correlation Coefficient: Simulation-Based Approach

Section 10.2

We will look at a small sample example to see if body temperature is associated with heart rate.

# Temperature and Heart Rate

## Hypotheses

- Null: There is no association between heart rate and body temperature. ( $\rho = 0$ )
- Alternative: There is a positive linear association between heart rate and body temperature. ( $\rho > 0$ )

$\rho = \text{rho}$

# Inference for Correlation with Simulation

## (Section 10.2)

1. Compute the observed statistic. (Correlation)
2. Scramble the response variable, compute the simulated statistic, and repeat this process many times.
3. Reject the null hypothesis if the observed statistic is in the tail of the null distribution.

# Temperature and Heart Rate

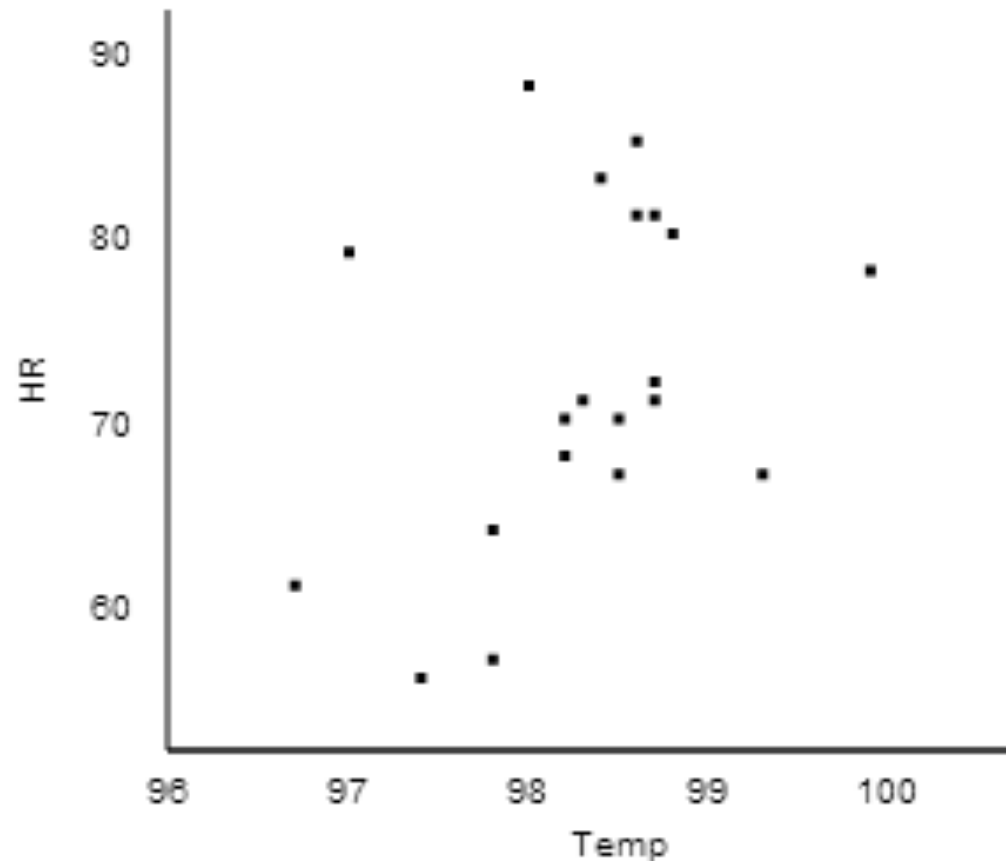
Collect the Data

Tmp	98.3	98.2	98.7	98.5	97.0	98.8	98.5	98.7	99.3	97.8
HR	72	69	72	71	80	81	68	82	68	65
Tmp	98.2	99.9	98.6	98.6	97.8	98.4	98.7	97.4	96.7	98.0
HR	71	79	86	82	58	84	73	57	62	89

# Temperature and Heart Rate

Explore the Data

$r = 0.378$



# Temperature and Heart Rate

- If there was no association between heart rate and body temperature, what is the probability we would get a correlation as high as 0.378 just by chance?
- If there is no association, we can break apart the temperatures and their corresponding heart rates. We will do this by shuffling one of the variables.

# Shuffling Cards

- Let's remind ourselves what we did with cards to find our simulated statistics.
- With two proportions, we wrote the response on the cards, shuffled the cards and placed them into two piles corresponding to the two categories of the explanatory variable.
- With two means we did the same thing except this time the responses were numbers instead of words.



# Dolphin Therapy

Non-improver	Improver	Improver
Non-improver	Improver	Improver
Non-improver	Improver	Improver
Non-improver	Improver	Improver
Non-improver	Improver	Improver

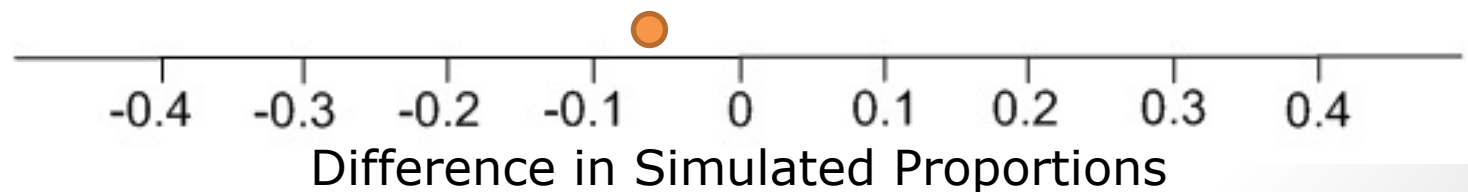
60.0%  
Improvers

# Control

Non-improver	Non-improver	Non-improver
Non-improver	Non-improver	Non-improver
Non-improver	Non-improver	Improver
Non-improver	Non-improver	Improver
Non-improver	Non-improver	Improver

20.0%  
Improvers

$$0.400 - 0.467 = -0.067$$



# Music

# No music

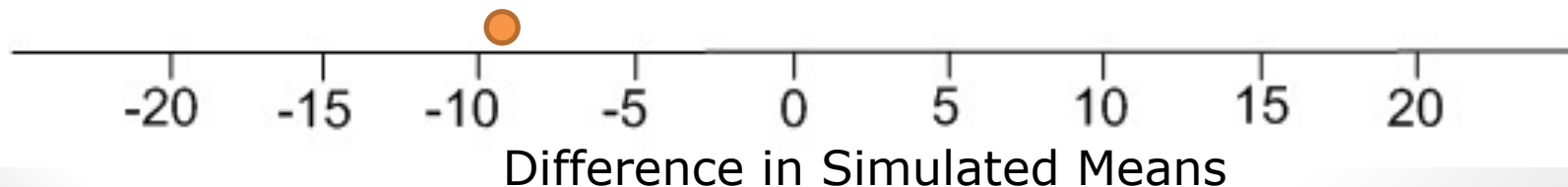
25.2	45.6
14.5	11.6
-7.0	18.6
12.6	12.1
34.5	30.5

mean = 6.38

-10.7	-10.7	10.0
4.5	9.6	
2.2	2.4	
21.3	21.8	
-14.7	7.2	

mean = 16.12

$$6.38 - 16.12 = -9.74$$



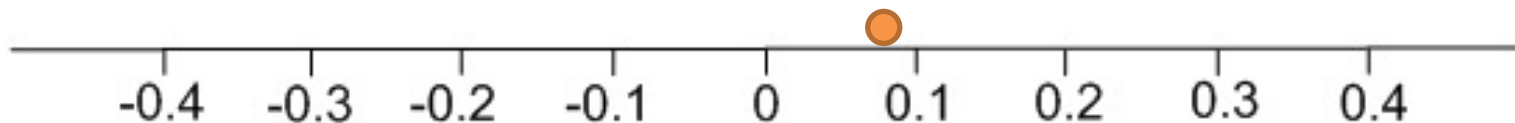
# Shuffling Cards

- Now how will this shuffling be different when both the response and the explanatory variable are quantitative?
- We can't put things in two piles anymore.
- We still shuffle values of the response variable, but this time place them next to two values of the explanatory variable.

# Body Temperature and Heart Rate

98.3° 72	98.2° 69	97.7° 72	98.5° 71	97.0° 80	98.8° 81	98.5° 68	98.7° 82	99.3° 68	97.8° 65
98.2° 71	99.9° 79	98.6° 86	98.6° 82	97.8° 58	98.4° 84	98.7° 73	97.4° 57	96.7° 62	98.0° 89

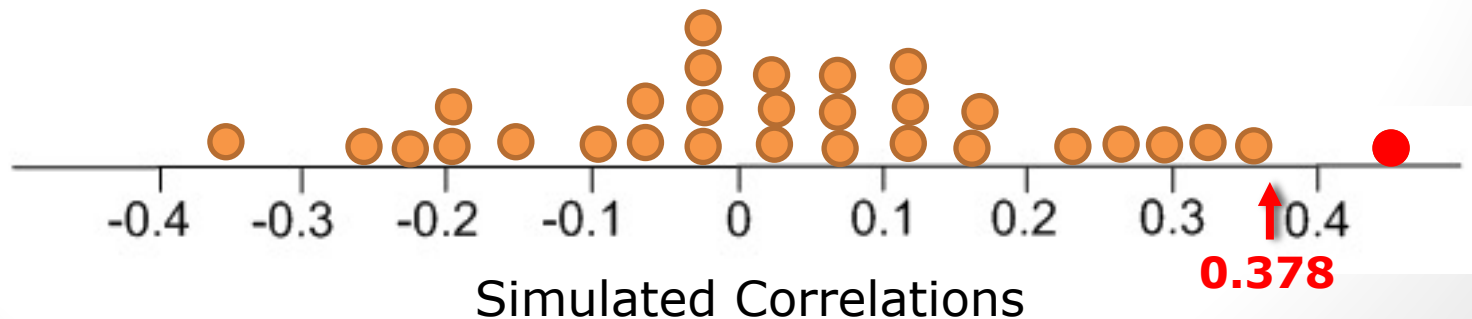
$r = 0.078$



Simulated Correlations

# More Simulations

Only one simulated statistic out of 30 was as large or larger than our observed correlation of 0.378, hence our p-value for this null distribution is  $1/30 \approx 0.03$ .

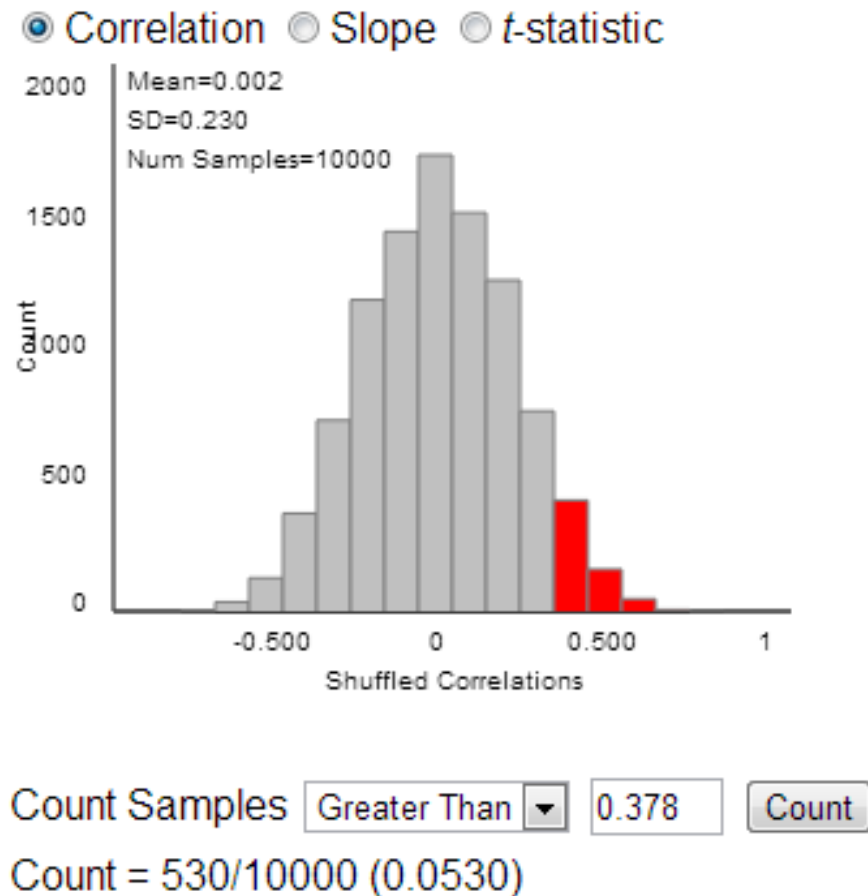


# Temperature and Heart Rate

- We can look at the output of 1000 shuffles with a distribution of 1000 simulated correlations.

# Temperature and Heart Rate

- Notice our null distribution is centered at 0 and somewhat symmetric.
- We found that 530/10000 times we had a simulated correlation greater than or equal to 0.378.



# Temperature and Heart Rate

- With a p-value of  $0.053 = 5.3\%$ , we almost but do not quite have statistical significance. We observe a positive linear association between body temperature and heart rate but this association is not statistically significant. Perhaps a larger sample should be investigated to get a better idea if the two variables are related or not.