

Stat 13, Intro. to Statistical Methods for the Life and Health Sciences.

1. Dolphins example, continued.
2. Comparing two proportions, theory-based example, smoking and gender.

Read chapter 5.

HW2 is due today, Wed, Feb12, 1159pm. 2.3.15, 3.3.18, and 4.1.23.

Midterm is Mon Feb24 in class.

The course website is <http://www.stat.ucla.edu/~frederic/13/W25> .

Swimming with Dolphins

- If the null hypothesis is true (no association between dolphin therapy and improvement) we would have 13 improvers and 17 non-improvers regardless of the group to which they were assigned.
- Hence the assignment doesn't matter and we can just randomly assign the subjects' results to the two groups to see what would happen under a true null hypothesis.

Swimming with Dolphins

- We can simulate this with cards
 - 13 cards to represent the improvers
 - 17 cards represent the non-improvers
- Shuffle the cards
 - put 15 in one pile (dolphin therapy)
 - put 15 in another (control group)

Swimming with Dolphins

- Compute the proportion of improvers in the Dolphin Therapy group
- Compute the proportion of improvers in the Control group
- The difference in these two proportions is what could just as well have happened under the assumption there is no association between swimming with dolphins and substantial improvement in depression.

Dolphin Therapy

Non-improver	Improver	Improver
Non-improver	Improver	Improver
Non-improver	Improver	Improver
Non-improver	Improver	Improver
Non-improver	Improver	Improver

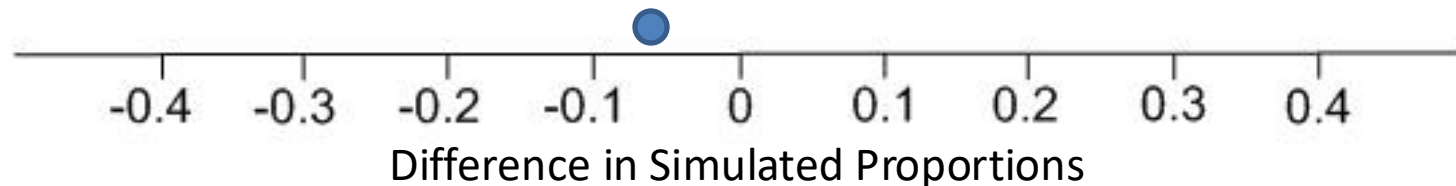
60.0% Improvers

Control

Non-improver	Non-improver	Non-improver
Non-improver	Non-improver	Non-improver
Non-improver	Non-improver	Improver
Non-improver	Non-improver	Improver
Non-improver	Non-improver	Improver

40.0% Improvers

$$0.400 - 0.467 = -0.067$$



Dolphin Therapy

Non-improver	Non-improver	Non-improver
Non-improver	Improver	Improver
Improver	Non-improver	Improver
Non-improver	Non-improver	Improver
Non-improver	Non-improver	Improver

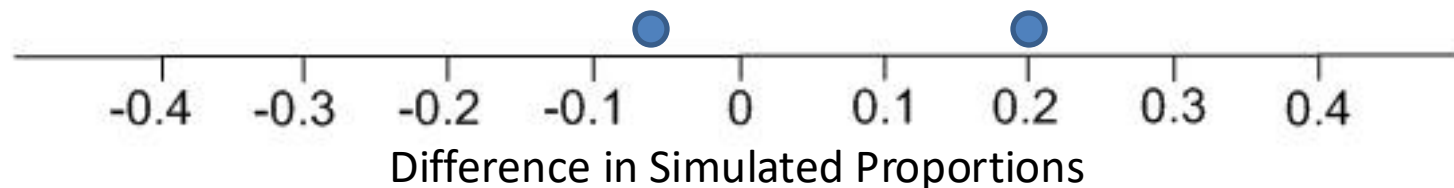
33.3% Improvers

Control

Non-improver	Improver	Non-improver
Non-improver	Non-improver	Improver
Non-improver	Non-improver	Improver
Improver	Non-improver	Improver
Improver	Improver	Non-improver

33.3% Improvers

$$0.533 - 0.333 = 0.200$$



Dolphin Therapy

Non-improver	Non-improver	Non-improver
Non-improver	Improver	Improver
Improver	Non-improver	Improver
Non-improver	Non-improver	Improver
Non-improver	Non-improver	Improver

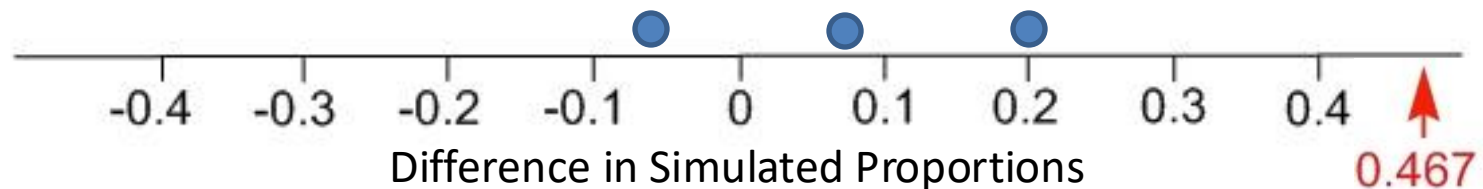
46.7% Improvers

Control

Non-improver	Improver	Non-improver
Non-improver	Non-improver	Improver
Non-improver	Non-improver	Improver
Improver	Non-improver	Improver
Improver	Improver	Non-improver

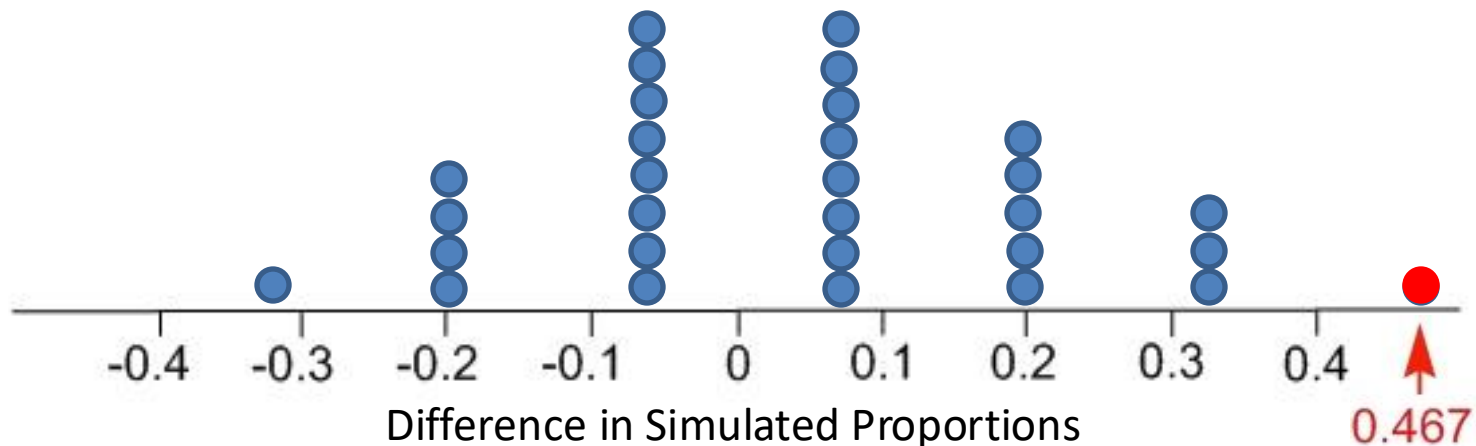
40.0% Improvers

$$0.467 - 0.400 = 0.067$$



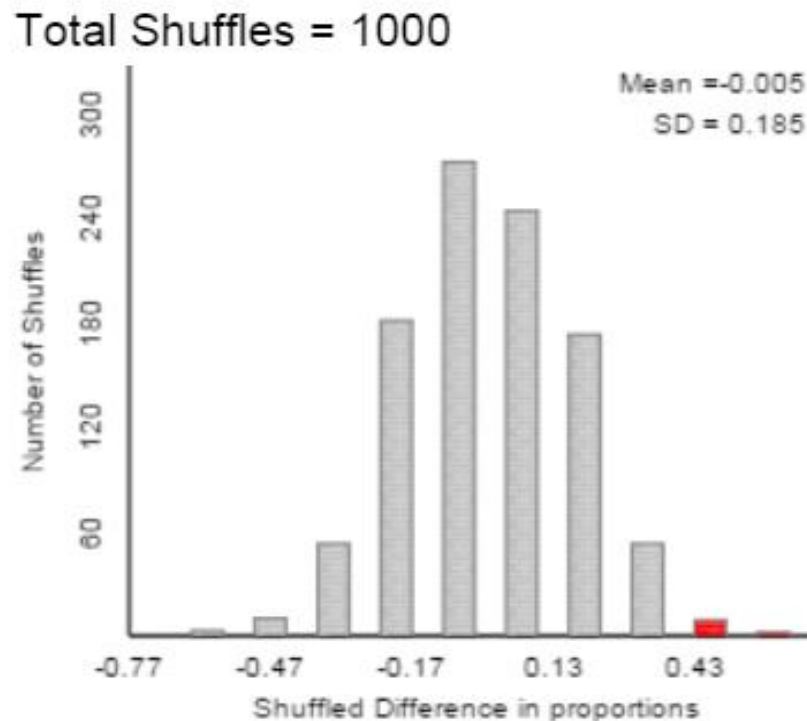
More Simulations

Only one simulated statistics out of 30 was as large or larger than our observed difference in proportions of 0.467, hence our p-value for this null distribution is $1/30 \approx 0.03$.



Swimming with Dolphins

- We did 1000 repetitions to develop a null distribution.



Swimming with Dolphins

- 13 out of 1000 results had a difference of 0.467 or higher (p-value = 0.013).
- 0.467 is $\frac{0.467 - 0}{0.185} \approx 2.52$ SE above zero.
- Using either the p-value or standardized statistic, we have strong evidence against the null and can conclude that the improvement due to swimming with dolphins was statistically significant.

Swimming with Dolphins

- A 95% confidence interval for the difference in the probability using the standard error from the simulations is $0.467 \pm 1.96(0.185) = 0.467 \pm 0.363$, or $(.104, .830)$.
- We are 95% confident that when allowed to swim with dolphins, the probability of improving is between 0.104 and 0.830 higher than when no dolphins are present.
- How does this interval back up our conclusion from the test of significance?

Swimming with Dolphins

- Can we say that the presence of dolphins *caused* this improvement?
 - Since this was a randomized experiment, and assuming everything was identical between the groups, we have strong evidence that dolphins were the cause
- Can we generalize to a larger population?
 - Maybe mild to moderately depressed 18-65 year old patients willing to volunteer for this study
 - We have no evidence that random selection was used to find the 30 subjects. "Outpatients, recruited through announcements on the internet, radio, newspapers, and hospitals."

2. Comparing two proportions.
Theory-Based Approach, and
smoking and gender example.

Section 5.3

Introduction

- Just as with a single proportion, we can often predict results of a simulation using a theory-based approach.
- The theory-based approach also gives a simpler way to generate a confidence intervals.
- The main new mathematical fact to use is the SE for the difference between two proportions is

$$\sqrt{\hat{p}(1 - \hat{p}) \left(\frac{1}{n_1} + \frac{1}{n_2} \right)} .$$

Parents' Smoking Status and their Babies' Gender

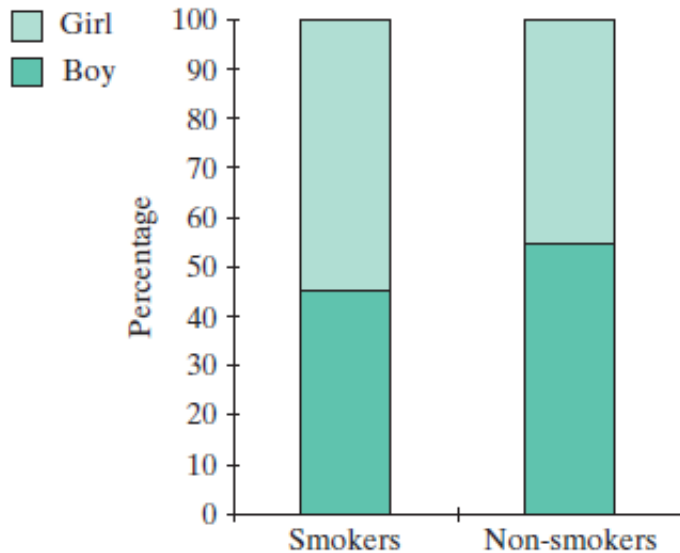
Example 5.3

Smoking and Gender

- How does parents' behavior affect the gender of their children?
- Fukuda et al. (2002) found the following in Japan.
 - Out of 565 births where both parents smoked more than a pack a day, 255 were boys. This is 45.1% boys.
 - Out of 3602 births where both parents did not smoke, 1975 were boys. This 54.8% boys.
 - In total, out of 4167 births, 2230 were boys, which is 53.5%.
- Other studies have shown a reduced male to female birth ratio where high concentrations of other environmental chemicals are present (e.g. industrial pollution, pesticides)

Smoking and Gender

- A segmented bar graph and 2-way table
- Let's compare the proportions to see if the difference is statistically significantly.



	Both Smoked	Neither Smoked
Boy	255 (45.1%)	1,975 (54.8%)
Girl	310	1,627
Total	565	3,602

Smoking and Gender

Null Hypothesis:

- There **is no association** between smoking status of parents and sex of child.
- The probability of having a boy **is the same** for parents who smoke and don't smoke.
- $\pi_{\text{smoking}} - \pi_{\text{nonsmoking}} = 0$

Smoking and Gender

Alternative Hypothesis:

- There **is an association** between smoking status of parents and sex of child.
- The probability of having a boy **is not the same** for parents who smoke and don't smoke
- $\pi_{\text{smoking}} - \pi_{\text{nonsmoking}} \neq 0$

Smoking and Gender

- What are the observational units in the study?
- What are the variables in this study?
- Which variable should be considered the explanatory variable and which the response variable?
- What is the parameter of interest?
- Can you draw cause-and-effect conclusions for this study?

Smoking and Gender

Using the 3S Strategy to assess the strength

1. Statistic:

- The proportion of boys born to nonsmokers minus the proportion of boys born to smokers is $0.548 - 0.451 = 0.097$.

Smoking and Gender

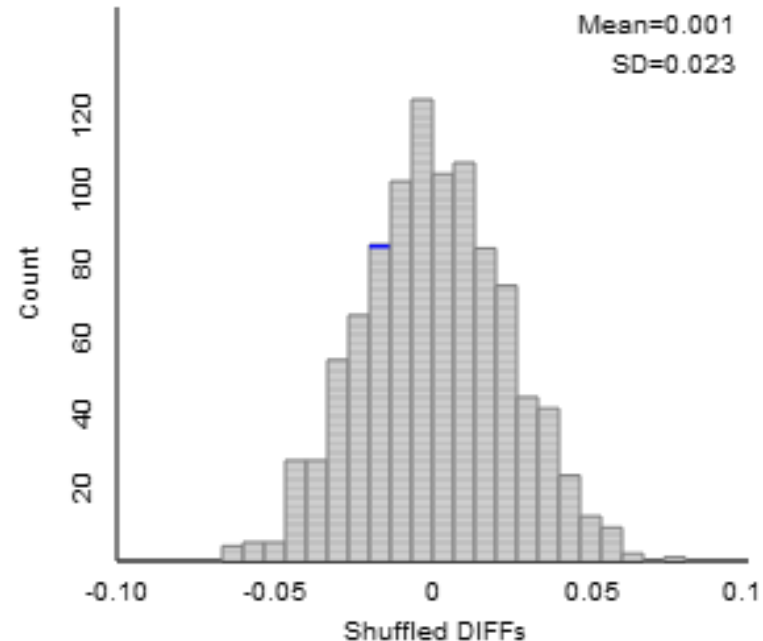
2. Simulate:

- Many repetitions of shuffling the 2230 boys and 1937 girls to the 565 smoking and 3602 nonsmoking parents
- Calculate the difference in proportions of boys between the groups for each repetition.
- Shuffling simulates the null hypothesis of no association

Smoking and Gender

3. Strength of evidence:

- Nothing as extreme as our observed statistic (≥ 0.097 or ≤ -0.097) occurred in 5000 repetitions,
- How many SEs is 0.097 above the mean?
 $Z = 0.097/0.023 = 4.22$
using simulations. What about using the theory-based approach?

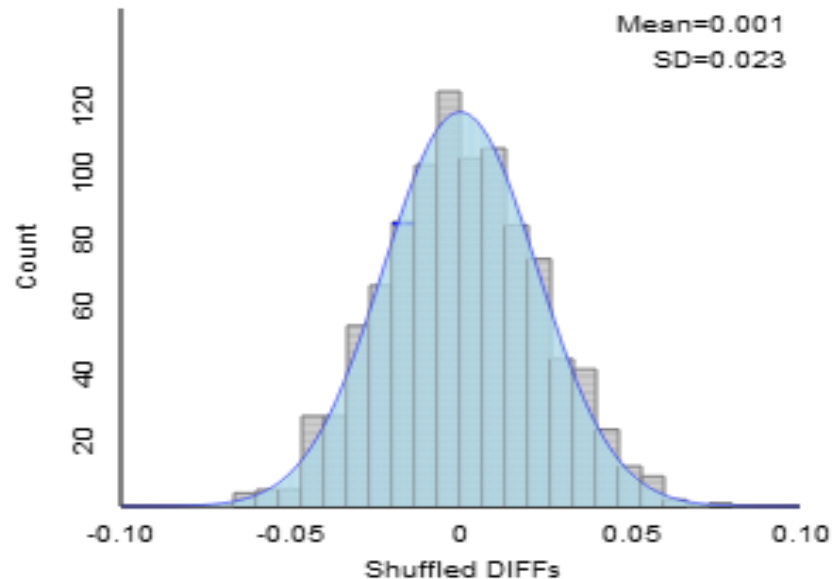


Count Samples Beyond

Count = 0/1000 (0.0000)

Smoking and Gender

- Notice the null distribution is centered at zero and is bell-shaped.
- This can be approximated by the normal distribution.



Formulas

- The theory-based approach yields $z = 4.30$.

$$z = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\hat{p}(1 - \hat{p}) \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}}$$

- Here $z = \frac{.548 - .451}{\sqrt{.535(1 - .535) \left(\frac{1}{3602} + \frac{1}{565} \right)}} = 4.30$.
- p-value is $2 * (1 - \text{pnorm}(4.30)) = 0.00171\%$.

Smoking and Gender

- Fukuda et al. (2002) found the following in Japan.
 - Out of 3602 births where both parents did not smoke, 1975 were boys. This is 54.8% boys.
 - Out of 565 births where both parents smoked more than a pack a day, 255 were boys. This is 45.1% boys.
 - In total, out of 4167 births, 2230 were boys, which is 53.5% boys.

Formulas

- How do we find the margin of error for the difference in proportions?

$$\text{Multiplier} \times \sqrt{\left(\frac{\hat{p}_1(1 - \hat{p}_1)}{n_1} + \frac{\hat{p}_2(1 - \hat{p}_2)}{n_2} \right)}$$

- The multiplier is from the normal distribution and is dependent upon the confidence level.
 - 1.645 for 90% confidence
 - 1.96 for 95% confidence
 - 2.576 for 99% confidence
- We can write the confidence interval in the form:
 - statistic \pm margin of error.

Smoking and Gender

- Our statistic is the observed sample difference in proportions, 0.097.
- Plugging in $1.96 \times \sqrt{\left(\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}\right)} = 0.044$, we get 0.097 ± 0.044 as our 95% CI.
- We could also write this interval as (0.053, 0.141).
- We are 95% confident that the probability of a boy baby where neither family smokes minus the probability of a boy baby where both parents smoke is between 0.053 and 0.141.

A clarification on the formulas

- For CIs, the margin of error for the difference in proportions is

$$\text{Multiplier} \times \text{SE, where SE} = \sqrt{\left(\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}\right)}$$

In testing, the null hypothesis is no difference between the two groups, so we use the SE

$$\sqrt{\left(\frac{\hat{p}(1-\hat{p})}{n_1} + \frac{\hat{p}(1-\hat{p})}{n_2}\right)}$$

where \hat{p} is the proportion in both groups combined. But in

CIs, we use the formula $\sqrt{\left(\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}\right)}$ because we are not assuming $\hat{p}_1 = \hat{p}_2$ with CIs.

Smoking and Gender

- How would the interval change if the confidence level was 99%?
- The SE = $\sqrt{\left(\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}\right)} = .0224$.
- Previously, for a 95% CI, it was $0.097 \pm 1.96 \times .0224 = 0.097 \pm 0.044$.
- For a 99% CI, it is $0.097 \pm 2.576 \times .0224 = 0.097 \pm 0.058$.

Smoking and Gender

- Written as the statistic \pm margin of error, the 99% CI for the difference between the two proportions is

$$0.097 \pm 0.058.$$

- Margin of error
 - 0.058 for the 99% confidence interval
 - 0.044 for the 95% confidence interval

Smoking and Gender

- How would the 95% confidence interval change if we were estimating

$$\pi_{\text{smoker}} - \pi_{\text{nonsmoker}}$$

instead of

$$\pi_{\text{nonsmoker}} - \pi_{\text{smoker}} ?$$

Smoking and Gender

- $(-0.141, -0.053)$ or -0.097 ± 0.044
instead of
- $(0.053, 0.141)$ or 0.097 ± 0.044 .
- The negative signs indicate the probability of a boy born to smoking parents is lower than that for nonsmoking parents.

Smoking and Gender

Validity Conditions of Theory-Based

- Same as with a single proportion.
- Should have at least 10 observations in each of the cells of the 2 x 2 table.

	Smoking Parents	Non-smoking Parents	Total
Male	255	1975	2230
Female	310	1627	1937
Total	565	3602	4167

Smoking and Gender

- The strong significant result in this study yielded quite a bit of press when it came out.
- Soon other studies came out which found no relationship between smoking and gender (Parazinni et al. 2004, Obel et al. 2003).
- James (2004) argued that confounding variables like social factors, diet, environmental exposure or stress were the reason for the association between smoking and gender of the baby. These are all confounded since it was an observational study. Different studies could easily have had different levels of these confounding factors.