

HW1 is 1.3, 1.10, 1.19, 1.20, 1.27.

1.3. Generate 100 observations from an autoregressive model.

Suppose we want to simulate  $x_t = 0.7 x_{t-1} + 0.6 x_{t-2} + w_t$ , where  $\sigma^2 = v(w_t) = 1$ .

And suppose we want to MA filter it generating

$$y_t = 0.5 x_{t-1} + 0.25 x_{t-2} + 0.25 x_{t-3}.$$

```
w = rnorm(150,0,1)
```

```
x = filter(w, filter=c(0.7,0.6), method="recursive")[-(1:50)]
```

```
y = filter(x, c(0.5,0.25,0.25), sides = 1)
```

```
plot.ts(x)
```

```
lines(y,lty=2)
```

1.10. Show the MSE is minimized when  $A = \rho(l)$ .

How do you show something is minimized?

1.19. Find the true autocovariance function of

$$x_t = \mu + w_t + \theta w_{t-1}.$$

$\gamma(h) = \text{cov}(x_t, x_{t+h})$ . See p17 for an example.

1.20. Simulate a process and find the sample acf. Use the R function `acf()`.  
See p29 for an example.

1.27. Suppose a process  $x_t$  is stationary with mean  $\mu$  and autocovariance  $\gamma(h)$ . What is  $E(x_t^2)$ ? What is  $E(x_{t+h}^2)$ ?