

Statistics 222, Spatial Statistics.

Outline for the day:

1. Exams.
2. Stoyan-Grabarnik statistic. Baddeley et al., 2005.
3. fitpoisstoyan.r
4. fitpoiscubicstoyan.r
5. fitpoisstoyancovariates.r
6. fithawkesstoyan.r

1. Exams.

1. d. 2.25.

2. a. $\frac{1}{4} \times \frac{1}{4} \times \frac{1}{2} = 1/32$.

3. f. $\text{gamma(large } h\text{)} - \text{gamma}(h \text{ near 0}) = 11 - 1 = 10$.

4. b. simple and λ doesn't depend on what other points have occurred.

5. e. $\log(3) + \log(3+50/\pi) - 30 - 2(.5) = -27$.

6. a. $E \sum \log \lambda - \int \lambda d\mu = E \int \log(\lambda) \lambda - \lambda d\mu$

$$= .5[(\log 10)(10)(10) - 100] + .5[(\log 20)(20)(10) - 200]$$

$$= 50 \log 10 + 100 \log 20 - 150 = 264.7025.$$

$$\begin{aligned}
7. \text{ g. } E \sum \log \lambda - \int \lambda d\mu &= E \int \lambda \log(\lambda) - \lambda d\mu \\
&= .5 \times .25 \times 10 \times (e+2e^2+3e^3+4e^4) - .5 \times 10 \times .25 \times (e+e^2+e^3+e^4) \\
&\quad + .5 \times .25 \times 10 \times (2e^2+3e^3+4e^4+5e^5) - .5 \times 10 \times .25 \times (e^2+e^3+e^4+e^5) \\
&= 1.25(e+2e^2+3e^3+4e^4) - 1.25(e+e^2+e^3+e^4) + 1.25(2e^2+3e^3+4e^4+5e^5) \\
&\quad - 1.25(e^2+e^3+e^4+e^5) \\
&= e(0) + e^2(2.5-1.25+2.5-1.25) + e^3(3.75-1.25+3.75-1.25) \\
&\quad + e^4(5-1.25+5-1.25) + e^5(6.25-1.25) \\
&= 2.5e^2 + 6e^3 + 7.5e^4 + 5e^5 = 1290.538.
\end{aligned}$$

8. f. You keep all the 3s, 4s, and 5s, plus $5/6$ of the 6s. So you expect to have $2.5(3+4+5+5) = 17 \times 2.5 = 42.5$ points kept. The kept points form a Poisson process, so $\text{var}(M(B)) = EM(B) = 42.5$.

$$\begin{aligned}
9. \text{ E. } \gamma(h) &= \rho(0) - \rho(h) \\
&= 1/(2\beta) - \exp(-\beta h)/(2\beta).
\end{aligned}$$

10. C. $E(D) = E \sum .4/\lambda = E \int .4/\lambda dN = E \int .4/\lambda \lambda d\mu = E \int .4 d\mu = 0.4 \times |B| = 4.$

2. Stoyan-Grabarnik statistic. Baddeley et al., 2005.

$$E \sum 1/\lambda_i = E \int 1/\lambda \lambda d\mu = E \int d\mu = |B|.$$

So, $\sum 1/\lambda_i - |B|$ should be close to zero.

What if we fit parameters by minimizing $(\sum 1/\lambda_i - |B|)^2$?

More specifically, imagine dividing up B into little grid cells, and within each cell, calculate this difference, $(\sum 1/\lambda_i - |B|)$, and find the parameters minimizing the sum of squares?