# **Homework 3**

## **Exercise 1**

THE JOINT POF OF YI AM 11:  $f(y_1, y_2) = f(y_1) \cdot f(y_2) = e' \cdot e' = e'$ (IND FORMOLIT)

LET U= X1/14 AND V=X

IF FOLLOWS THAT YZ=V AND Y\_= UV

JACOBIAN:

$$\frac{1}{\sqrt{1+1}} = \frac{1}{\sqrt{1+1}} = \frac{1}{\sqrt{1+1+1}} = \frac{1}{\sqrt{$$

TO FIND POF OF U INTFORMTE THE JOINT POF W.R.T. V.

$$f(u) = \int_{0}^{\infty} e^{-\frac{1}{2}x} dv = 1.$$

EXPRISE 2:

(a) KNN(0.1), YNN(0.1) X, Y ARG

[NORPHMENT

FOINT POF OF X, Y:  $f(x,y) = f(x). f(y) = \sqrt{2}$   $= \frac{1}{2} - \frac{1}{2} \times \frac{1}{2} - \frac{1}{2} \times \frac{1}{2}$   $= \frac{1}{2} - \frac{1}{2} \times \frac{1}{2} - \frac{1}{2} \times \frac{1}{2}$   $= \frac{1}{2} - \frac{1}{2} \times \frac{1}{2} - \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2}$   $= \frac{1}{2} - \frac{1}{2} \times \frac{1}{2} - \frac{1}{2} \times \frac{1}{2} \times$ 

 $f(u,v) = \frac{1}{20} \cdot \frac{1}{20} \cdot$ 

THIS IS SIMPUFIED TO: f(4,v) = 1/2 / 1/2 = 1/2 / 1/2 / 1/2 | e = 1/2 / 1/2 | | e = 1/2 / 1/2 | e = 1/2 / 1/2

EXERCISE 3:  

$$1 \sim beta(x, 0)$$
 ) Yorbeta(x+b, t)  
 $1 \sim beta(x+b)$  )  $1 \sim beta(x+b)$   $1 \sim beta($ 

### **Exercise 4**

(a) ODF OR R.

$$P(R \leq Y) = 1 - P(R > Y) = 1 - P(X = 0)$$
PARTICLES

N SPHERE
WITH VOLUME ATIP)

$$= 1 - \frac{\lambda_s}{4\pi r^3} = 1 - \frac{4\pi r^3}{4\pi r^3}$$

$$f(m) = 4\pi r^3$$

(4) Let 
$$U = R^{3}$$
 $F(u) = P(U = u) = P(R^{3} = u)$ 
 $= P(R = u^{3}) = F(u^{3})$ 
 $= P(R = u^{3}) = F(u^{3})$ 
 $= P(R = u^{3}) = F(u^{3})$ 
 $= P(u) = \frac{1}{3}u^{3} + \lambda \pi u$ 
 $= \frac{1}{3}u^{3} + \lambda u$ 
 $= \frac{1}{3}u^{3} +$ 

AM EU = 420

X1~ X1, X2~ X/2 1-1-X1/2 12-1-X1/2  $f(x_1,x_1) = f(x_1) f(x_1) = \frac{x_1^2 e}{\Gamma(\frac{x_1}{2}) 2^{r_1 k}} \cdot \frac{x_2}{\Gamma(\frac{x_2}{2}) 2^{r_2 k}}$  $J = \begin{vmatrix} \frac{\partial Y_1}{\partial x_1} & \frac{\partial Y_1}{\partial x_2} \\ \frac{\partial Y_2}{\partial x_1} & \frac{\partial Y_2}{\partial x_2} \\ \frac{\partial Y_2}{\partial x_2} & \frac{\partial Y_2}{\partial x_2} \\ \frac{\partial Y_2}{\partial x_1} & \frac{\partial Y_2}{\partial x_2} \\ \frac{\partial Y_2}{\partial x_2} & \frac{\partial$  $Y_1 = \frac{\chi_1}{\chi_1}$   $\chi_1 = \frac{\gamma_1 \gamma_2}{1 + \gamma_1}$   $\chi_2 = \frac{\gamma_2}{1 + \gamma_1}$   $\chi_3 = \frac{\gamma_2}{1 + \gamma_1}$  $\frac{Y_{1} = X_{1} + X_{1}}{f(Y_{1})X_{2}} = \frac{\frac{Y_{2}}{I + Y_{1}}}{\frac{Y_{1}^{2} - I}{I + Y_{1}}} = \frac{\frac{Y_{2}}{I + Y_{1}}}{\frac{Y_{2}^{2} - I}{I + Y_{1}}} = \frac{Y_{2}}{I + Y_{1}}}{\frac{Y_{2$  $= \frac{\frac{r_{1}-1}{2} - \frac{r_{1}+r_{2}}{2}}{\Gamma(\frac{r_{1}}{2})\Gamma(\frac{r_{2}}{2})} \cdot \frac{\frac{r_{1}+r_{2}}{2}}{\Gamma(\frac{r_{1}+r_{2}}{2})} \cdot \frac{r_{1}+r_{2}}{\Gamma(\frac{r_{1}+r_{2}}{2})} \frac{r_{1}+r_{2}}{2}$ = {(41). {(4). .: 41, 4 ARE IND RPENDA AND Y2~XXI+Y2

SINCE XI IND OF XI (GIVEN) XI/r, IND OF X3/r3

AND XI IND OF XITX2 XITX2

### **Exercise 6**

(a), 
$$P(X_1,...,X_{r-1}|X_r) = P(X_1,...,X_r)$$

$$= \frac{N!}{x_1! \cdot x_2! \cdot ... \cdot x_r!} P(X_r) \frac{1}{x_r} P(X_r) \frac$$

#### Exercise 7

$$X_i \mid P_i \sim \text{Beavour}(P_i^*)$$
,  $P_i \sim \text{Beta}(\alpha, \beta)$ 

(a) 
$$I. E X_i = E \left( E(X_i/P_i) \right) = E P_i = \frac{\lambda}{\lambda + B}$$

$$E ZX_i = N \frac{\lambda}{\lambda + B}$$

$$2. VAR(X_i) = E \left( VAR(X_i/P_i) \right) + VAR(E(X_i/P_i))$$

$$= E[P_i(F_i)] + VAR(P_i)$$

$$= \frac{\chi}{\chi+8} = \left(\frac{\chi^2}{(\chi+6)^2} + \frac{\chi}{(\chi+6)^2} + \frac{\chi}{(\chi+6)$$

(b) 
$$\chi_i \mid P_i \sim b \; (n_i, P_i) \; , \; P_i \sim beta(q_i \theta)$$

WHERE MR(Xi) = Ni 
$$\frac{dB(d+B+Ni)}{(a+B)}$$

#### **Exercise 8**

COF OF 
$$Q = P(X_i)$$

$$= P(PX_i \leq P)$$

$$= P(-h_1X_i \leq P)$$

$$= P(-h_1X_i - h_1X_i) > h_1P)$$

$$= P(-h_1X_i - h_1X_i) \sim \exp(i) \qquad (-f_1/-h_1P)$$

$$= \sum_{i=1}^{n} h_i \sim F(h_i)$$

$$= \sum_{i=1}^{n} h_i \sim F(h_i)$$