

University of California, Los Angeles
Department of Statistics

Statistics 13

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Exam 2
21 November 2014

Name: _____

UCLA ID: _____

Section: _____

Problem 1 (25 points)

Answer the following questions:

- a. A missile protection system consists of n radar sets operating independently, each with probability 0.90 of detecting a missile entering a zone. If $n = 5$ and a missile enters the zone what is the probability that exactly 4 radar sets detect the missile?

- b. Refer to question (a). How large must n be if we require that the probability of detecting a missile that enters the zone be 0.999?

- c. A true-false test consists of 50 questions. How many does a student have to get right to convince you that he/she is not just guessing? Please explain.

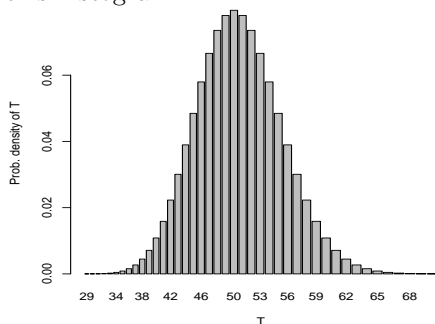
- d. Only 4% of people have Type AB blood. Suppose donors arrive independently at the UCLA Blood and Platelet Center. What is the probability that we find the 3rd Type AB blood donor on the 8th trial?

- e. Suppose blood donors arrive at the UCLA Blood and Platelet Center according to the Poisson distribution at the rate of $\lambda = 10$ per hour. What is the probability that in the next 30 minutes at least two blood donors will arrive?

Problem 2 (25 points)

Answer the following questions:

- a. The acidity of soils is measured by pH, which may range from 0 (high acidity) to 14 (high alkalinity). A soil scientist wants to estimate the average pH for a large field by randomly selecting $n = 40$ samples. Suppose $\sigma = 0.75$. Find the probability that the sample mean of the 40 pH measurements will be within 0.2 unit of the true mean pH of the field.
- b. Refer to question (a). Suppose the scientist would like the sample mean to be within 0.1 of the true mean with probability 90%. How many sample should the scientist take?
- c. We discussed in class that when two independent large samples are selected, the difference in the sample means $(\bar{X} - \bar{Y})$ according to the central limit theorem follows approximately the normal distribution. The flow of water through soil depends on, among other things, the porosity of the soil. For the comparison of two types of sandy soil, $n_1 = 50$ measurements and $n_2 = 100$ measurements are to be taken from two populations. Assume that $\sigma_1^2 = 0.01$ and $\sigma_2^2 = 0.02$. Find the probability that the difference between the sample means will be within 0.05 unit of the difference between the population means μ_1 and μ_2 .
- d. A population has mean $\mu = 1.25$ and standard deviation $\sigma = 2$. Repeated samples each one of size $n = 40$ are selected from this population. It is claimed that the histogram below represents the distribution of the total (T) of these 40 observations. Clearly explain if there is anything wrong with this histogram.



- e. Refer to question (d). Find the 10th percentile of the distribution of T .

Problem 3 (25 points)

Normal temperature (degrees Fahrenheit) readings (x) and heart rates (beats per minute) of 32 males were used in this problem. The regression output of y on x is given below. Note: Several values are missing! You are also given: $\sum_{i=1}^n x_i = 3142.4$, $var(x) = 0.4077$, $\bar{y} = 74.5313$, $var(y) = 37.2$ and $r = 0.2194$.

```
> q <- lm(a$rate ~ a$temperature)
> summary(q)
```

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)		167.135	-0.786	
a\$temperature				

Answer the following questions:

a. Find $\hat{\beta}_0$.

b. Find $\hat{\beta}_1$.

c. Is there a linear association between rate and temperature? Use $\alpha = 5\%$.

d. Approximate the p-value using your t table for testing $H_0 : \beta_0 = 0$ against the alternative $H_0 : \beta_0 \neq 0$.

e. Please list few nice properties about the least squares estimates $\hat{\beta}_0$ and $\hat{\beta}_1$.

