

University of California, Los Angeles
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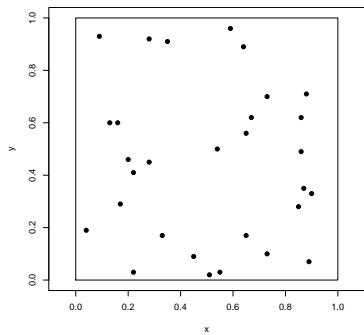
Statistics C173/C273

Instructor: Nicolas Christou

Plot ecdf against cdf for point pattern data

Consider the following coordinates of 30 events distributed over the unit square as shown on the graph below.

x	y
[1,]	0.54 0.50
[2,]	0.67 0.62
[3,]	0.64 0.89
[4,]	0.45 0.09
[5,]	0.90 0.33
[6,]	0.51 0.02
[7,]	0.04 0.19
[8,]	0.87 0.35
[9,]	0.89 0.07
[10,]	0.85 0.28
[11,]	0.17 0.29
[12,]	0.35 0.91
[13,]	0.13 0.60
[14,]	0.86 0.49
[15,]	0.73 0.10
[16,]	0.28 0.92
[17,]	0.88 0.71
[18,]	0.73 0.70
[19,]	0.20 0.46
[20,]	0.33 0.17
[21,]	0.65 0.56
[22,]	0.59 0.96
[23,]	0.09 0.93
[24,]	0.65 0.17
[25,]	0.22 0.41
[26,]	0.16 0.60
[27,]	0.55 0.03
[28,]	0.28 0.45
[29,]	0.22 0.03
[30,]	0.86 0.62



The nearest neighbor distances (NND) are the following:

```
[1] 0.125 0.063 0.086 0.092 0.036 0.041 0.164 0.036
[9] 0.163 0.071 0.130 0.071 0.030 0.130 0.106 0.071
[17] 0.092 0.100 0.054 0.144 0.063 0.086 0.190 0.106
[25] 0.054 0.030 0.041 0.072 0.178 0.092
```

Now generate a vector of distances r that will help us construct the empirical cumulative distribution function (ecdf) and the theoretical cumulative distribution function (cdf). The range of the NND values is $(0.03, 0.19)$, so let's use the following $r = (0.04, 0.06, 0.08, 0.10, 0.12, 0.14, 0.16, 0.18, 0.20)'$. The following table gives **ecdf** and **cdf**. Note: Assume that the random process has $\lambda = 30$.

r	Number of $NND \leq r$	ecdf: $\hat{G}(r) = \frac{\text{col2}}{30}$	cdf: $G_0(r) = 1 - e^{-\lambda\pi r^2}$
0.04	4	$\frac{4}{30} = 0.133$	$1 - \exp(-\lambda\pi 0.04^2) = 0.140$
0.06	8	$\frac{8}{30} = 0.267$	$1 - \exp(-\lambda\pi 0.06^2) = 0.288$
0.08	14	$\frac{14}{30} = 0.467$	$1 - \exp(-\lambda\pi 0.08^2) = 0.453$
0.10	20	$\frac{20}{30} = 0.667$	$1 - \exp(-\lambda\pi 0.10^2) = 0.610$
0.12	22	$\frac{22}{30} = 0.733$	$1 - \exp(-\lambda\pi 0.12^2) = 0.743$
0.14	25	$\frac{25}{30} = 0.833$	$1 - \exp(-\lambda\pi 0.14^2) = 0.842$
0.16	26	$\frac{26}{30} = 0.867$	$1 - \exp(-\lambda\pi 0.16^2) = 0.910$
0.18	29	$\frac{29}{30} = 0.967$	$1 - \exp(-\lambda\pi 0.18^2) = 0.953$
0.20	30	$\frac{30}{30} = 1.000$	$1 - \exp(-\lambda\pi 0.20^2) = 0.977$

Finally we plot $\hat{G}(r)$ against $G_0(r)$ to get the following plot:

