

#5-1

⑤

$$(a) P(X=3 \text{ and } Y=30) = \frac{7M}{100M} = \boxed{0.07}$$

Ans

(b)	X	0	1	2	3
	P(X)	A	B	C	D

$$A = (1M + 2M + 5M) / 100M = \boxed{0.08}$$

$$B = (3M + 6M + 10M) / 100M = \boxed{0.19}$$

$$C = (18M + 21M + 15M) / 100M = \boxed{0.54}$$

$$D = (7M + 8M + 4M) / 100M = \boxed{0.19}$$

	Y	30	45	70
	P(Y)	A	B	C

$$A = (1M + 3M + 18M + 7M) / 100M = \boxed{0.29}$$

$$B = (2M + 6M + 21M + 8M) / 100M = \boxed{0.37}$$

$$C = (5M + 10M + 15M + 4M) / 100M = \boxed{0.34}$$

$$(c) P(X, Y) \stackrel{?}{=} P(X) P(Y)$$

$$\text{Pick } X=3 \text{ and } Y=30. P(3, 30) = 0.07$$

$$P(3) = 0.19, P(30) = 0.29$$

$$\text{So } P(3)P(30) = (0.19)(0.29) = 0.0551$$

$\therefore X$ and Y are NOT independent

$$(d) \mu_X = 0(0.08) + 1(0.19) + 2(0.54) + 3(0.19) = \boxed{1.84}$$

$$\sigma_X = \sqrt{(0-1.84)^2(0.08) + (1-1.84)^2(0.19) + (2-1.84)^2(0.54) + (3-1.84)^2(0.19)}$$

$$= \boxed{0.8212}$$

