

HW#10

- A. $H_0: \text{mean height} = 69$
 $H_a: \text{mean height} > 69$
- B. $E(\bar{X}) = E(X)$
 $\text{SD}(\bar{X}) = \text{SD}(X)/\sqrt{n} = \text{SD}(X)/10$
- C. a) null hypothesis $H_0: \text{diff} = 0$
Alternative hypothesis $H_a: \text{diff} > 0$
- b) According to the null hypothesis, $E(\bar{X}) = E(X) = 0$
- c) \bar{X} of observed value = $(1.2+2.4+\dots+1.4)/10 = 1.58$
- d) SD of observed differences = $\sqrt{[(\sum(x-\bar{x})^2)/(n-1)]} = 1.23$
- e) Using table in Appendix F, $P(T > 1.38) = 0.1$ $P(T > 2.82) = 0.01$ (df=9)
- f) Observed value of T = $(1.58-0)/(1.23/\sqrt{10}) = 4.06$
- g) The smallest value of the observed value of T for which we would reject the null hypothesis is 1.83
- h) Yes, reject the null hypothesis

Section 12.2 P616

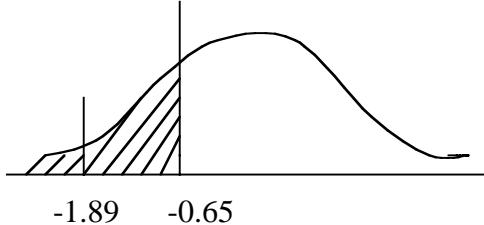
3. $H_0: \mu = 50$

$H_a: \mu < 50$

$\bar{x} = 49.25$, sample has 8 plots, SD of sample = 3.25,

$T = (49.25 - 50)/(3.25/\sqrt{8}) = -0.65$

According to the alternative hypothesis, $P\text{value} = P(T < -0.65)$



df=7, if significant level is 5%, Pvalue > 0.05, so fail to reject the null hypothesis.
(t=1.89 at 5% significant level with 7 degree of freedom)

4. $\bar{X} = (62 + 83 + \dots + 266 + 277)/17 = 146.5$

$\text{SD} = \sqrt{[(\sum(x-\bar{x})^2)/(n-1)]} = \sqrt{(68078.25/16)} = 260.9/4 = 65.229$

$T = (146.5 - 160)/(65.229/\sqrt{17}) = -0.853$

$H_0: \bar{x} = 160$

$H_a: \bar{x} > 160$

Df=16, pvalue = $P(T > -0.853) > 0.05$, fail to reject the null hypothesis.
(t=1.75 at 5% significant level with 16 degree of freedom.)

5. $H_0: \text{diff} = 0$ $H_a: \text{diff} > 0$

$T = (5 - 0)/(3.4/\sqrt{14}) = 5.5$

Df=13, pvalue = $P(T > 5.5) < 0.05$, so reject the null hypothesis.

(t=1.77 at 5% significant level with 13 degree of freedom.)